

# geoR : Package for Geostatistical Data Analysis

## *introductory session and snapshots*

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The package `geoR` provides functions for geostatistical data analysis using the software `R`. This document illustrates some (**but not all** !) of the capabilities of the package.

The objective is to familiarise the reader with the `geoR`'s commands and show some of the plots which can be produced.

The commands used here are simply basic examples of the package handling. We did not attempt to perform a definitive data analysis. Typically, default arguments are used for the function calls and the user is encouraged to inspect other function arguments. For example, to see all the available arguments for the function `variog` type:

```
> args(variog)
```

We refer to the `geoR` documentation for more details on the functions included in `geoR`.

## 1. STARTING A SESSION AND LOADING DATA

After starting an `R` session, load `geoR` with the command:

```
> library(geoR)
```

If the installation directory for the package is other than the default location for `R` packages, type:

```
> library(geoR, lib.loc="PATH_TO_geoR"),
```

where "PATH\_TO\_geoR" is the path to the directory where `geoR` was installed. If the package is correctly loaded the following message will be displayed:

```
-----  
geoR: a package for geostatistical analysis in R  
geoR is now loaded  
-----
```

Typically, data is stored as an object (a list) of the class "geodata". An object of this class contains at least the coordinates of data locations and the data values. We refer to the documentation for the functions `as.geodata` and `read.geodata` for more information on how to import/convert data and on the definitions of the class "geodata".

We use the data set `s100` included in the **geor** distribution for the examples included in this document. This data set can be loaded by typing:

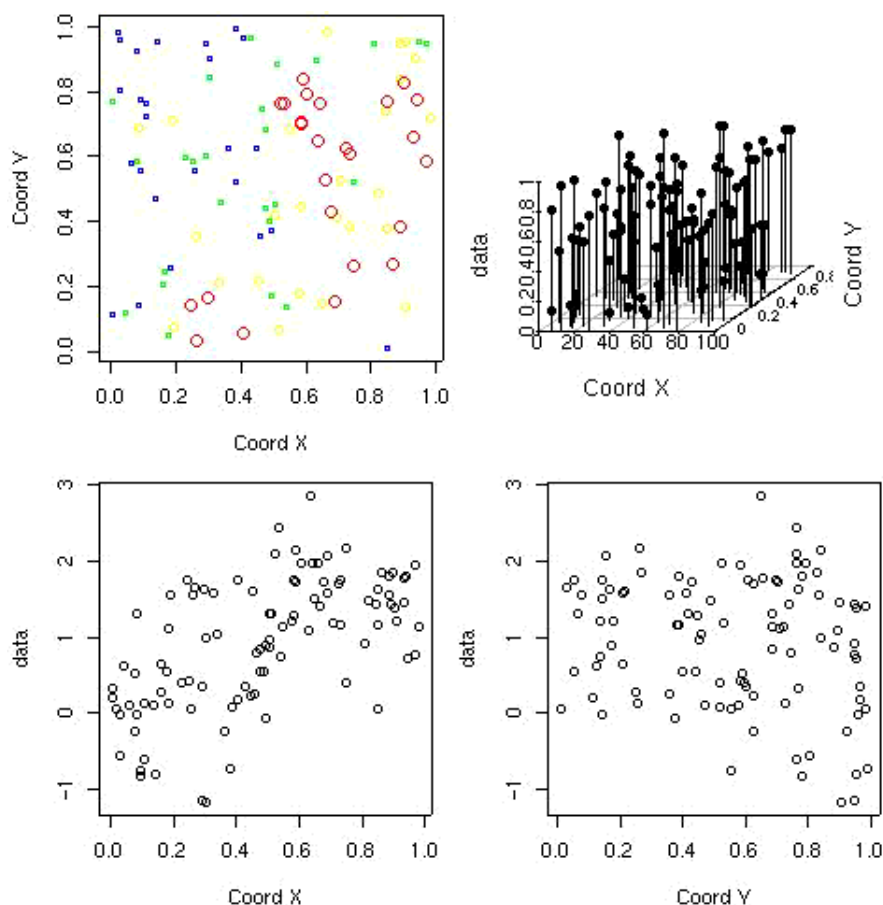
```
> data(s100)
```

## 2. EXPLORATORY TOOLS

### 1. Plotting data locations and values

The function `plot.geodata` shows a 2 x 2 display with data locations (top plots) and data *versus* coordinates (bottom plots). For an object of the class "geodata" the plot is produced by the command:

```
> plot(s100)
```

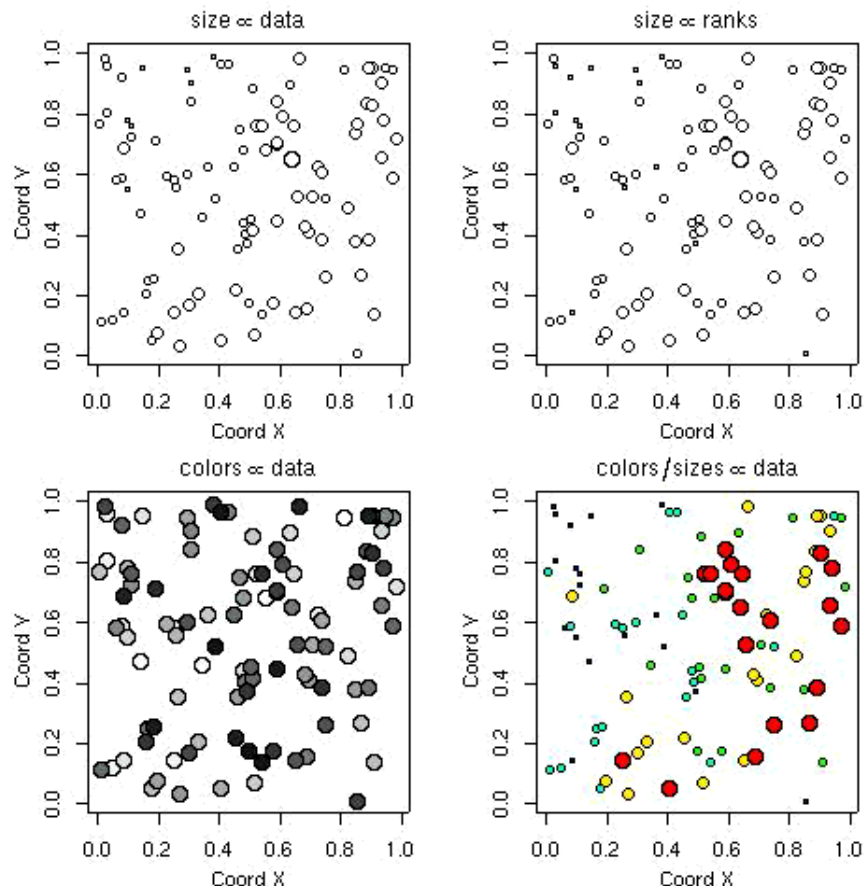


Notice that the top-right plot is produced using the package **scatterplot3d**. If this package is not installed a histogram of the data replaces this plot.

The function `points.geodata` produces a plot showing the data locations. Alternatively, points indicating the data locations can be added to a current plot. There are options to specify point sizes, patterns and colors, which can be set to be proportional to the data values or specified quantiles.

Some examples of graphical outputs are illustrated by the commands and corresponding plots as seeing below.

```
> par(mfrow = c(2,2))
> points(s100, xlab = "Coord X", ylab = "Coord Y")
> points(s100, xlab = "Coord X", ylab = "Coord Y", pt.size =
"rank.prop")
> points(s100, xlab = "Coord X", ylab = "Coord Y", cex.max = 1.7, col
= gray(seq(1, 0.1, l=100)), pt.size = "equal")
> points(s100, pt.sizes = "quintile", xlab = "Coord X", ylab = "Coord
Y")
> par(mfrow = c(1,1))
```



## 2. Empirical variograms

Empirical variograms are calculated using the function `variog`. There are options for the *classical* or *modulus* estimator.

Results can be returned as variogram clouds, binned or smoothed variograms.

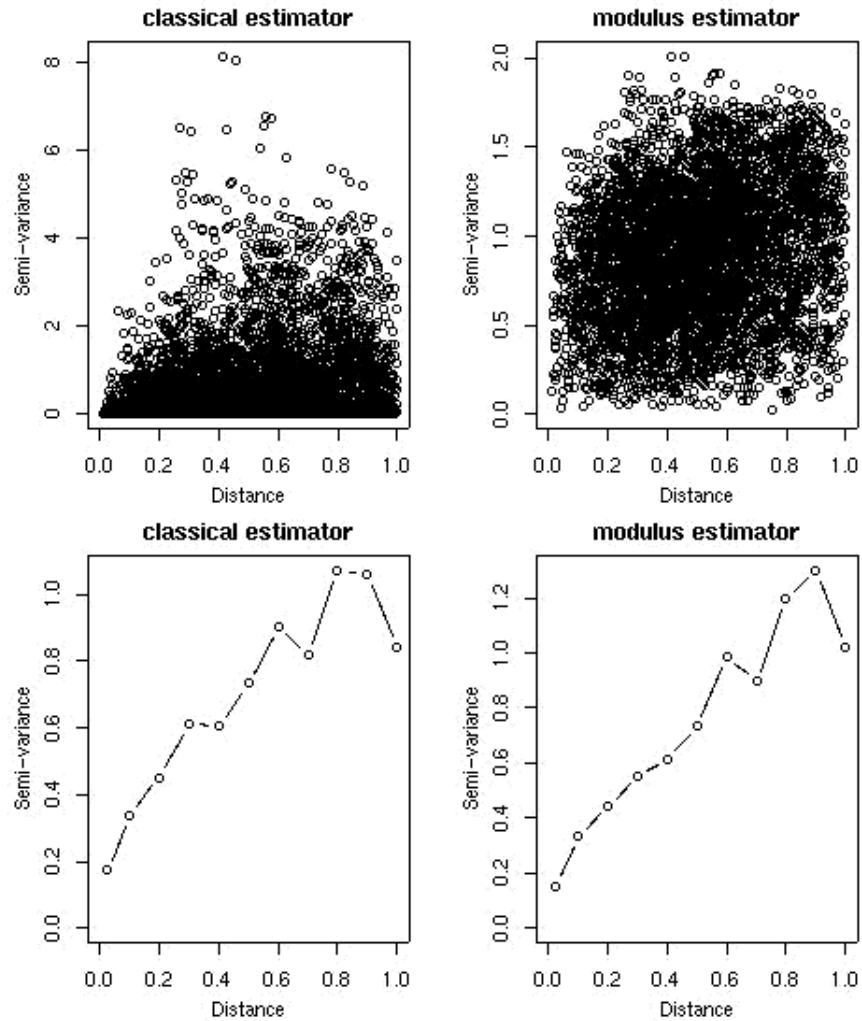
```
> cloud1 <- variog(s100, option = "cloud", max.dist=1)
> cloud2 <- variog(s100, option = "cloud", estimator.type = "modulus",
max.dist=1)
> bin1 <- variog(s100, uvec=seq(0,1,l=11))
> bin2 <- variog(s100, uvec=seq(0,1,l=11), estimator.type= "modulus")

> par(mfrow=c(2,2))
> plot(cloud1, main = "classical estimator")
```

```

> plot(cloud2, main = "modulus estimator")
> plot(bin1, main = "classical estimator")
> plot(bin2, main = "modulus estimator")

```



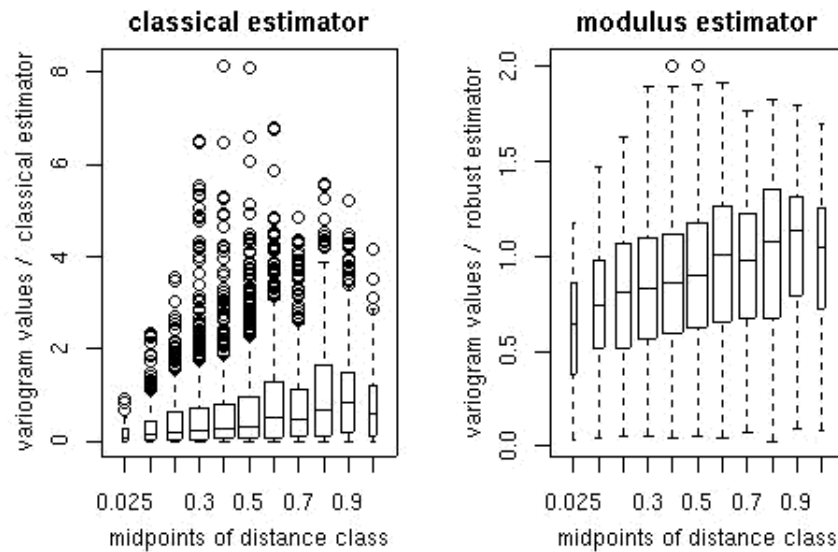
Furthermore, the points of the variogram clouds can be grouped in classes of distances ("bins") and displayed using a box-plot for each bin.

```

> bin1 <- variog(s100, uvec = seq(0,1,l=11), bin.cloud = T)
> bin2 <- variog(s100, uvec = seq(0,1,l=11), estimator.type =
"modulus", bin.cloud = T)

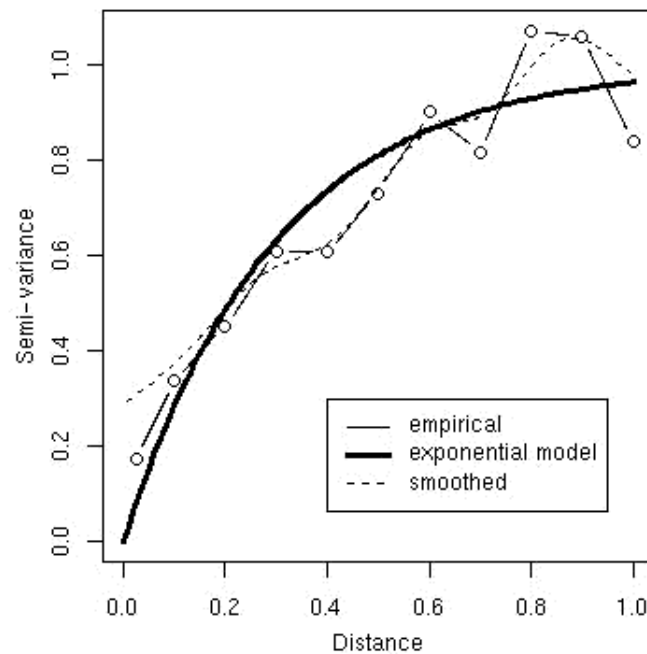
> par(mfrow = c(1,2))
> plot(bin1, bin.cloud = T, main = "classical estimator")
> plot(bin2, bin.cloud = T, main = "modulus estimator")

```



Theoretical and empirical variograms can be plotted and visually compared. For example, the figure below shows the theoretical variogram model used to simulate the data `s100` and two estimated variograms.

```
> bin1 <- variog(s100, uvec = seq(0,1,l=11))
> plot(bin1)
> lines.variomodel(list(nugget = 0, cov.pars = c(1,0.3), max.dist = 1,
cov.model = "exp"), lwd = 3)
> smooth <- variog(s100, option = "smooth", max.dist = 1, n.points =
100, kernel = "normal", band = 0.2)
> lines(smooth, type = "l", lty = 2)
> legend(0.4, 0.3, c("empirical", "exponential model", "smoothed"),
lty = c(1,1,2), lwd = c(1,3,1))
```



### 3. PARAMETER ESTIMATION

Model parameters can be estimated by using:

- *least squares fit of empirical variograms*: with options for ordinary (OLS) and weighted (WLS) least squares
- *likelihood based methods*: with options for maximum likelihood (ML) and restricted maximum likelihood (REML)

Bayesian methods are also implemented and will be presented in Section 5.

The nugget effect parameter can be estimated or set to a fixed value. The same applies for smoothness, anisotropy and transformation parameters. Options for taking trends into account are also included. Trends can be specified as polynomial functions of the coordinates and/or linear functions of given covariates.

The commands below shows models fitted by different methods with options for fixed or estimated nugget parameter. Features not illustrated here include estimation of trends, anisotropy, smoothness and Box-Cox transformation parameter.

```
# Fitting models with nugget fixed to zero
> ml <- likfit(s100, ini = c(0.5,0.5), fix.nugget = T)
> reml <- likfit(s100, ini = c(0.5,0.5), fix.nugget = T, method = "RML")
> ols <- olsfit(bin1, ini = c(0.5,0.5), fix.nugget = T)
> wls <- wlsfit(bin1, ini = c(0.5,0.5), fix.nugget = T)

# Fitting models with a fixed value for the nugget
> ml.fn <- likfit(s100, ini = c(0.5,0.5), fix.nugget = T, nugget = 0.15)
> reml.fn <- likfit(s100, ini = c(0.5,0.5), fix.nugget = T, nugget = 0.15,
method = "RML")
> ols.fn <- olsfit(bin1, ini = c(0.5,0.5), fix.nugget = T, nugget = 0.15)
> wls.fn <- wlsfit(bin1, ini = c(0.5,0.5), fix.nugget = T, nugget = 0.15)

# Fitting models estimated nugget
> ml.n <- likfit(s100, ini = c(0.5,0.5), nug = 0.5)
> reml.n <- likfit(s100, ini = c(0.5,0.5), nug = 0.5, method = "RML")
> ols.n <- olsfit(bin1, ini = c(0.5,0.5), nugget=0.5)
> wls.n <- wlsfit(bin1, ini = c(0.5,0.5), nugget=0.5)

# Now, plotting fitted models against empirical variogram
> par(mfrow = c(1,3))

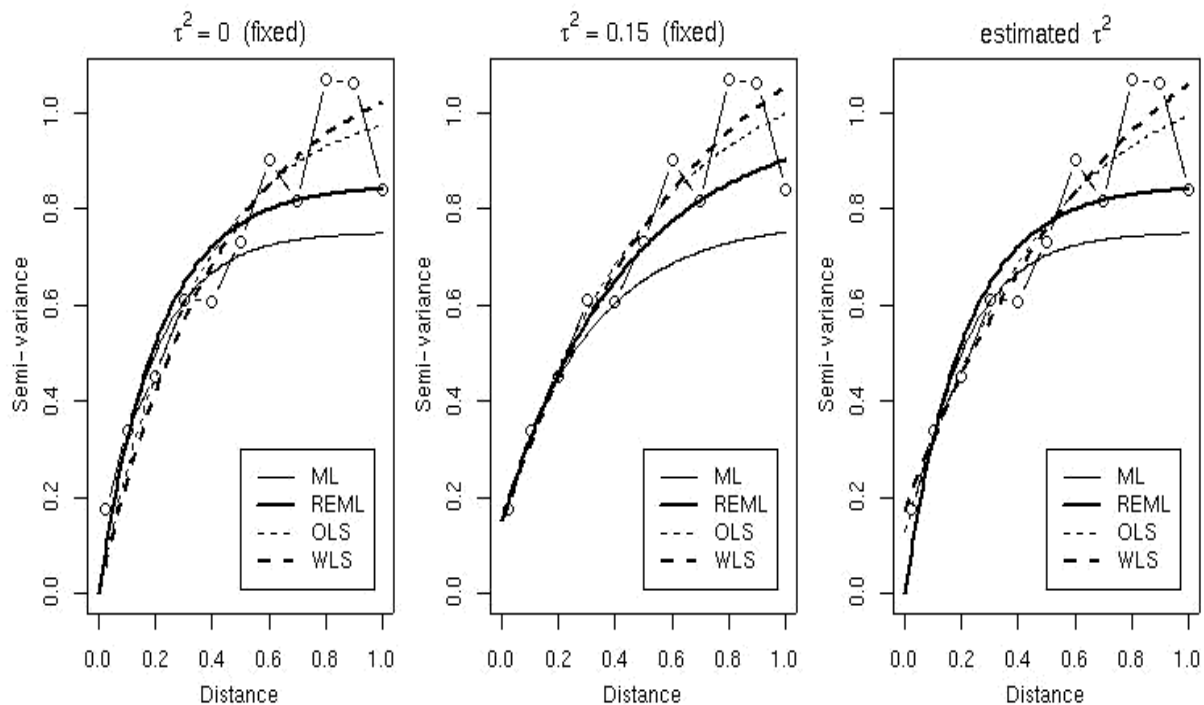
> plot(bin1, main = expression(paste(tau^2 == 0, " (fixed)")))
> lines(ml, max.dist = 1)
> lines(reml, lwd = 2, max.dist = 1)
> lines(ols, lty = 2, max.dist = 1)
> lines(wls, lty = 2, lwd = 2, max.dist = 1)
> legend(0.6, 0.3, legend = c("ML", "REML", "OLS", "WLS"), lty =
c(1,1,2,2), lwd = c(1,2,1,2))

> plot(bin1, main = expression(paste(tau^2 == 0.15, " (fixed)")))
> lines(ml.fn, max.dist = 1)
> lines(reml.fn, lwd = 2, max.dist = 1)
> lines(ols.fn, lty = 2, max.dist = 1)
> lines(wls.fn, lty = 2, lwd = 2, max.dist = 1)
> legend(0.6, 0.3, legend = c("ML", "REML", "OLS", "WLS"), lty =
c(1,1,2,2), lwd = c(1,2,1,2))
```

```

> plot(bin1, main = expression(paste("estimated ", tau^2))
> lines(ml.n, max.dist = 1)
> lines(reml.n, lwd = 2, max.dist = 1)
> lines(ols.n, lty = 2, max.dist = 1)
> lines(wls.n, lty = 2, lwd = 2, max.dist = 1)
> legend(0.6, 0.3, legend = c("ML", "REML", "OLS", "WLS"), lty =
c(1,1,2,2), lwd = c(1,2,1,2))

```



Summary methods have been written to summarize the resulting objects.  
 For example, for the model with estimated nugget fitted by maximum likelihood, typing:

```
> ml.n
```

will produce the output:

```

likfit: estimated model parameters:
      beta   tausq sigmasq   phi
0.7766  0.0000  0.7517  0.1827

likfit: maximised log-likelihood = -83.5696

```

and for more detailed summary is obtained with:

```

> summary(ml.n)

Summary of the parameter estimation
-----
Estimation method: maximum likelihood

Parameters of the mean component (trend):
      beta
0.7766

Parameters of the spatial component:
      correlation function: exponential

```

```

      (estimated) variance parameter sigmasq (partial sill) = 0.7517
      (estimated) cor. fct. parameter phi (range parameter) = 0.1827
anisotropy parameters:
      (fixed) anisotropy angle = 0 ( 0 degrees )
      (fixed) anisotropy ratio = 1

Parameter of the error component:
      (estimated) nugget = 0

Transformation parameter:
      (fixed) Box-Cox parameter = 1 (no transformation)

Maximised Likelihood:
      log.L n.params      AIC      BIC
-83.5696   4.0000 -87.5696 -92.7799

Call:
likfit(geodata = s100, ini.cov.pars = c(0.5, 0.5), nugget = 0.5)

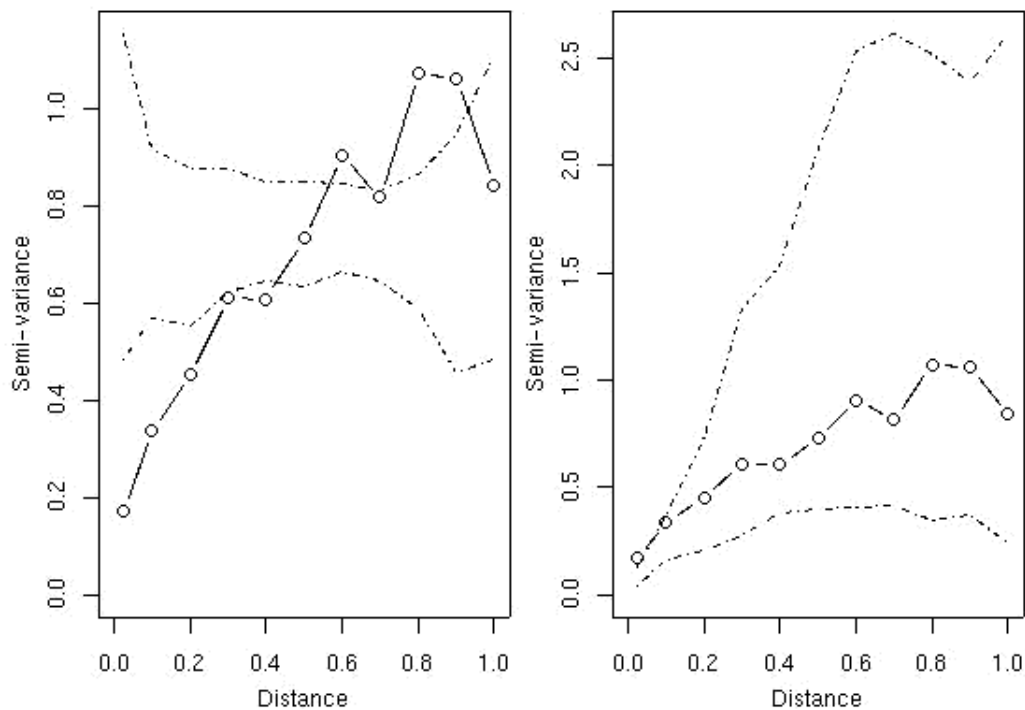
```

Two kinds of variogram *envelops* can be computed by simulation and are illustrated in the next figure. The plot on the left-hand side shows envelops based on permutation of the data values across the data locations. The envelops shown on the right-hand side are based on simulations from a given set of model parameters, in this example the parameter estimates from the *WLS* variogram fit.

```

> env.mc <- variog.mc.env(s100, obj.var=bin1)
> env.model <- variog.model.env(s100, obj.var=bin1, model=wls)
> par(mfrow=c(1,2))
> plot(bin1, envelope=env.mc)
> plot(bin1, envelope=env.model)

```

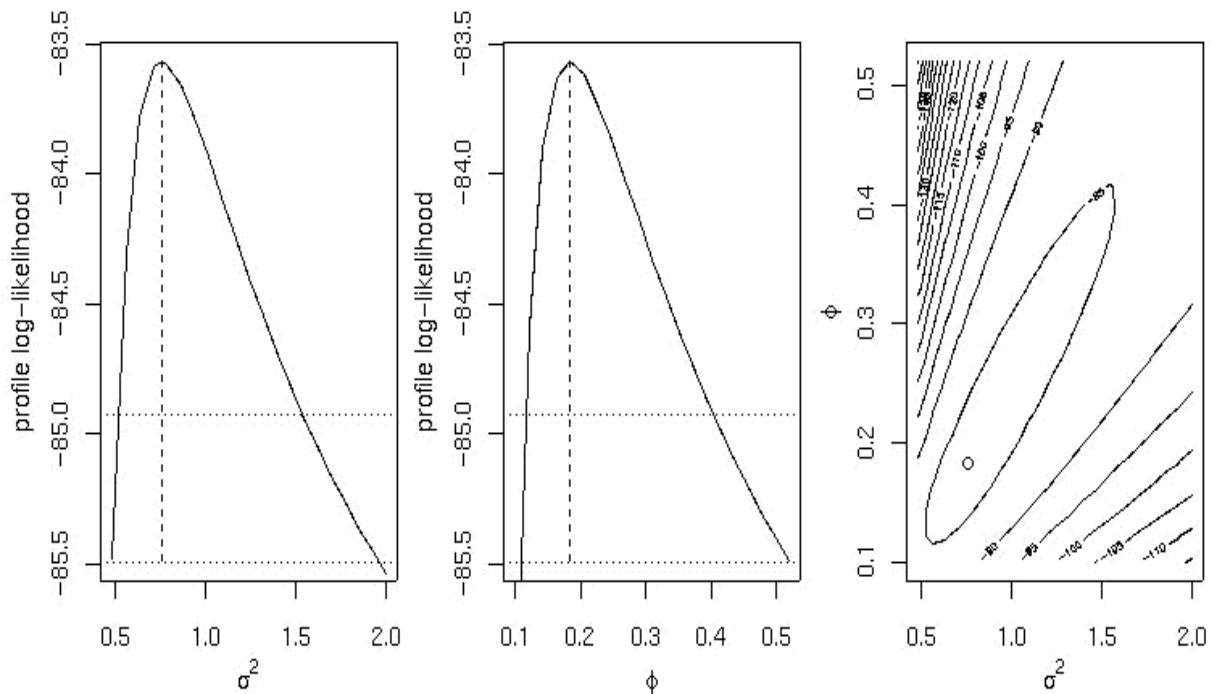


Profile likelihoods (1-D and 2-D) are computed by the function `proflik`. Here we show the



profile likelihoods for the covariance parameters of the model without nugget effect previously fitted by `likfit`.

```
> prof <- proflik(ml, geodata = s100, sill.val = seq(0.48, 2, l=21),
range.val = seq(0.1, 0.52, l=21))
> par(mfrow=c(1,3))
> plot(prof, nlevels=16)
```



## 4. SPATIAL INTERPOLATION

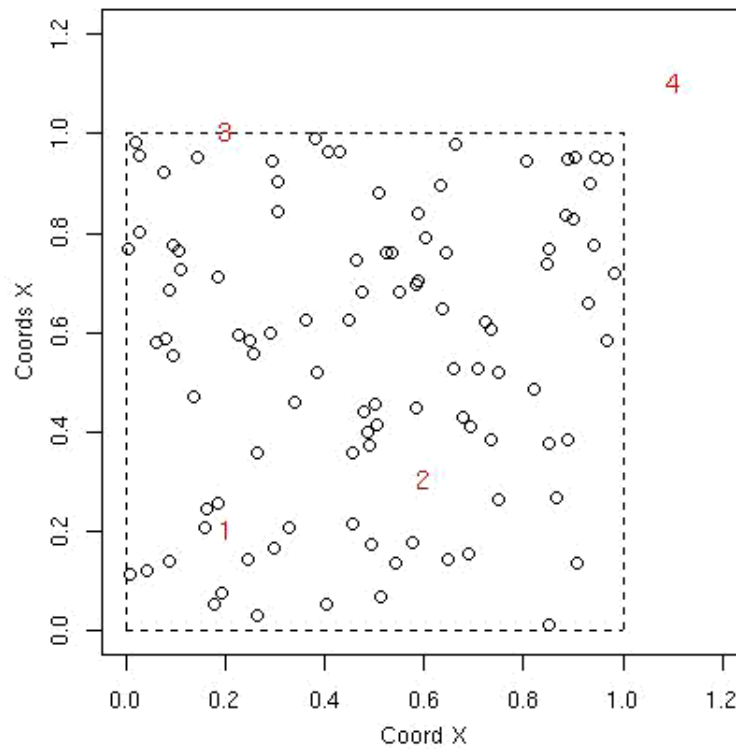
Conventional geostatistical spatial interpolation (*kriging*) can be performed with options for:

- *Simple kriging*
- *Ordinary kriging*
- *Trend (universal) kriging*
- *External trend kriging*

There are additional options for Box-Cox transformation (and back transformation of the results) and anisotropic models. Simulations can be drawn from the resulting predictive distributions if requested.

As a first example consider the prediction at four locations labeled 1, 2, 3, 4 and indicated in the figure below.

```
> plot(s100$coords, xlim=c(0,1.2), ylim=c(0,1.2))
> loci <- matrix(c(0.2, 0.6, 0.2, 1.1, 0.2, 0.3, 1.0, 1.1), ncol=2)
> text(loci, as.character(1:4))
> segments(c(0,0,0,1), c(0,0,1,0), c(1,0,1,1), c(0,1,1,1), lty=2)
```



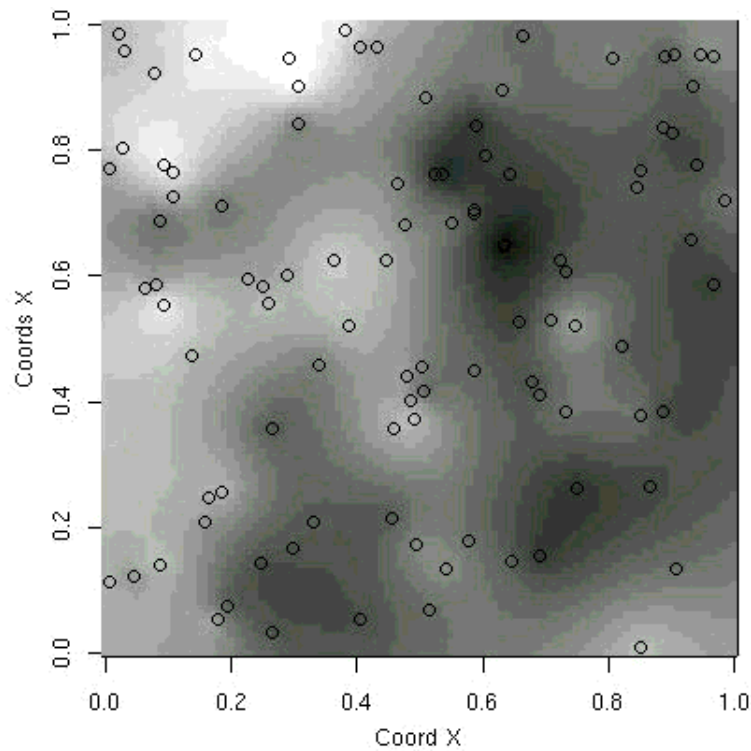
The command to perform *ordinary kriging* using the parameters estimated by weighted least squares with nugget fixed to zero would be:

```
> kc4 <- krige.conv(s100, locations = loci, krige = krige.control(cov.pars
= wls$cov.pars))
```

The output is a list including the predicted values (`kc4$predict`) and the kriging variances (`kc4$krige.var`).

Consider now a second example. The goal is to perform prediction on grid covering the area and display the results. Again, we use ordinary kriging. The commands are:

```
# defining the grid
> pred.grid <- expand.grid(seq(0,1, l=101), seq(0,1, l=101))
# kriging calculations
> kc <- krige.conv(s100, locations = pred.grid, krige =
krige.control(cov.pars = ml$cov.pars))
# displaying predicted values
> image.kriging(kc, loc = pred.grid, coords = s100$coords,
col=gray(seq(1,0.1,l=30)))
```



## 5. BAYESIAN ANALYSIS

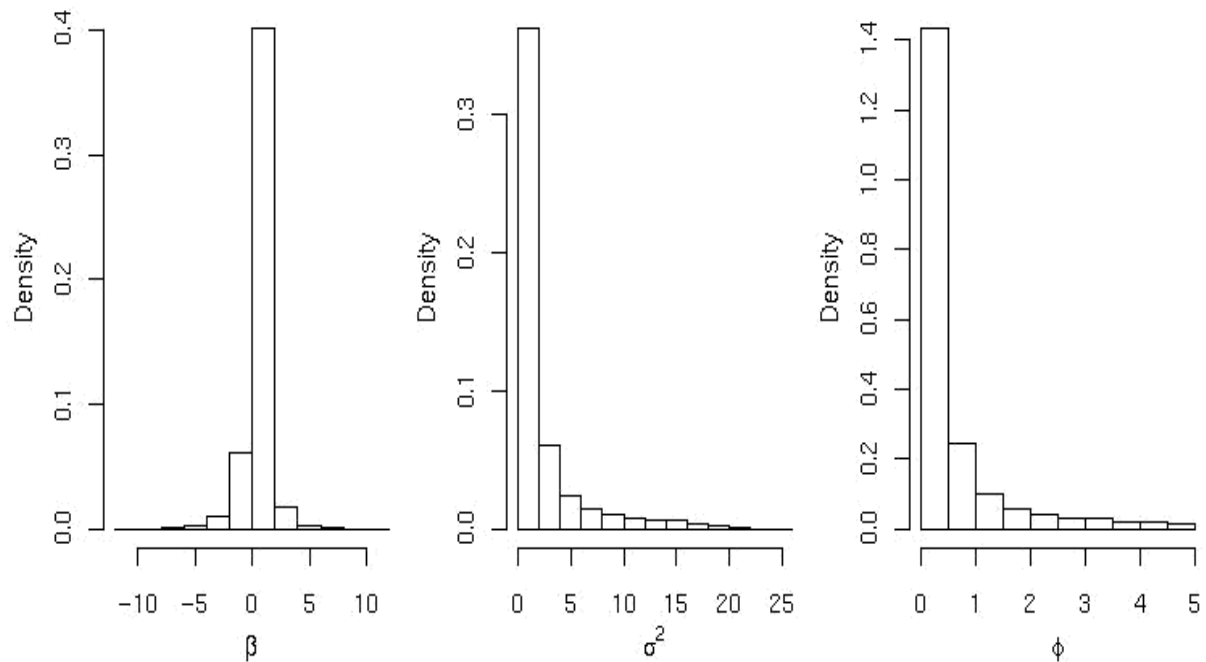
Bayesian analysis for Gaussian models is implemented by the function `krige.bayes`. It can be performed for different "degrees of uncertainty", meaning that model parameters can be set to be regarded as fixed or random.

As an example consider a model without nugget and including uncertainty in the mean, sill and range parameters. Prediction at the four locations indicated above is performed by typing a command like:

```
> bsp4 <- krige.bayes(sl00, loc = loci, prior =
prior.control(range.discrete = seq(0,5,l=501), range.prior="rec"),
output=output.control(n.post=10000))
```

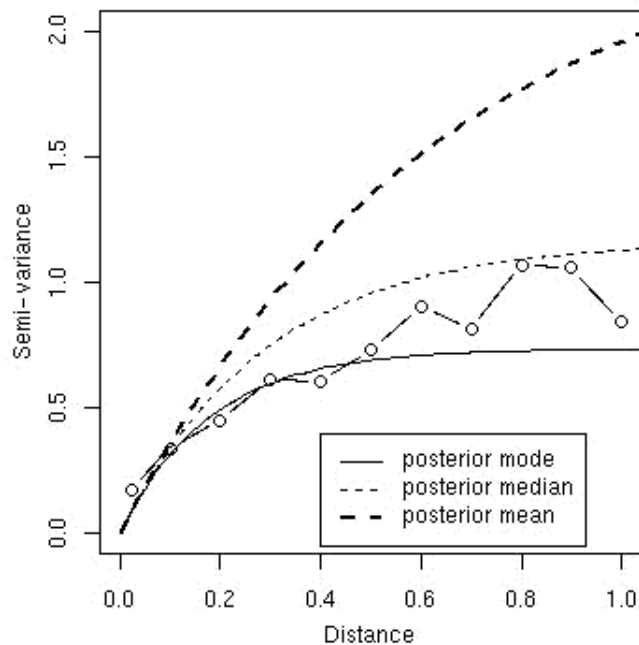
Histograms showing posterior distribution for the model parameters can be plotted by typing:

```
> hist(bsp4$posterior$beta.sam, main="", xlab=expression(beta), prob=T)
> hist(bsp4$posterior$sigma.sq.sam, main="", xlab=expression(sigma^2),
prob=T)
> hist(bsp4$posterior$phi.sam, main="", xlab=expression(phi), prob=T)
```



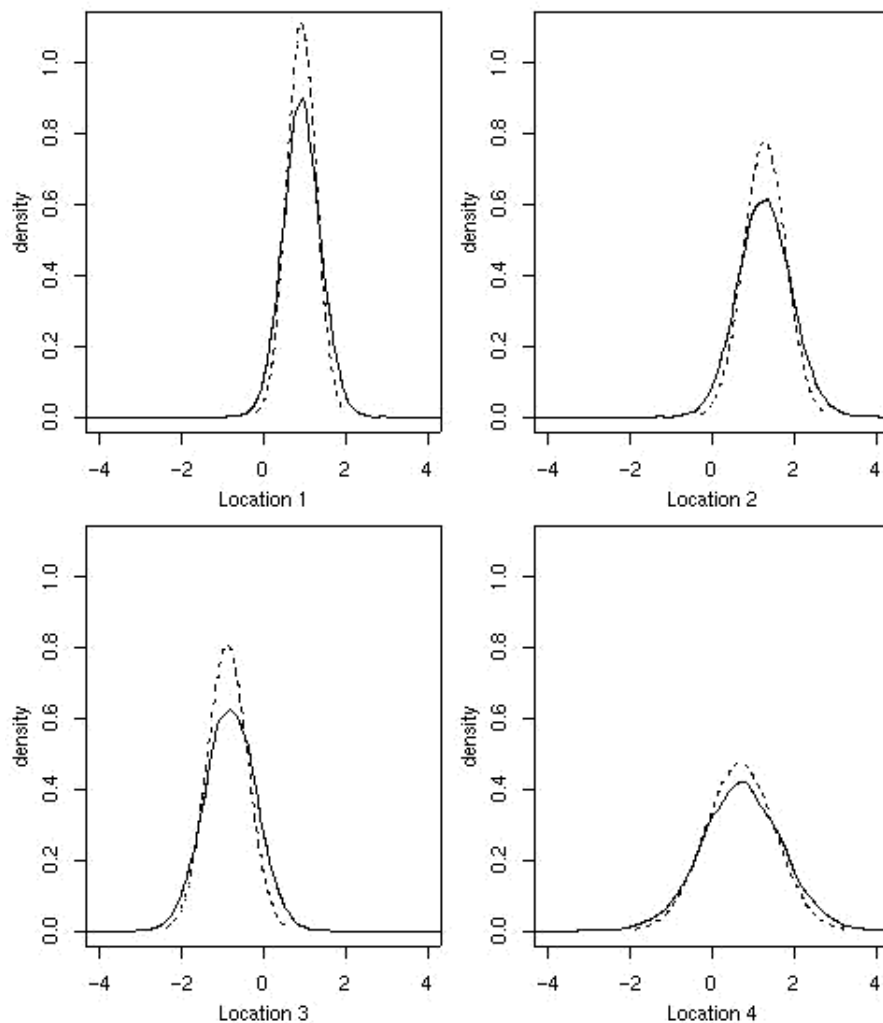
Using summaries of these posterior distributions (means, medians or modes) we can check the "estimated Bayesian variograms" against the empirical variogram, as shown in the next figure. Notice that it is also possible to compare these estimates with other fitted variograms as the ones computed in Section 3.

```
> plot(bin1, ylim = c(0,2))
> lines(bsp, max.dist = 1.2, ylim = c(0,2))
> lines(bsp, max.dist = 1.2, summ = "median", lty = 2)
> lines(bsp, max.dist = 1.2, summ = "mean", lwd = 2, lty = 2)
> legend(0.4, 0.3, legend = c("posterior mode", "posterior median",
"posterior mean"), lty = c(1,2,2), lwd = c(1,1,2))
```



The next figure shows predictive distributions at the four selected locations. Dashed lines shown Gaussian distributions with mean and variance given by results of ordinary kriging obtained in Section 4. The full lines corresponds to the Bayesian prediction. The plot shows results of density estimation using samples from the predictive distributions.

```
> for(i in 1:4){
> kpx <- seq(kc4$pred[i] - 3*sqrt(kc4$krige.var[i]), kc4$pred[i]
+3*sqrt(kc4$krige.var[i]), l=100)
> kpy <- dnorm(kpx, mean=kc4$pred[i], sd=sqrt(kc4$krige.var[i]))
> bp <- density(bsp4$predic$sim[i,])
> rx <- range(c(kpx, bp$x))
> ry <- range(c(kpy, bp$y))
> plot(cbind(rx, ry), type="n", xlab=paste("Location", i), ylab="density",
xlim=c(-4, 4), ylim=c(0,1.1))
> lines(kpx, kpy, lty=2)
> lines(bp)}
```



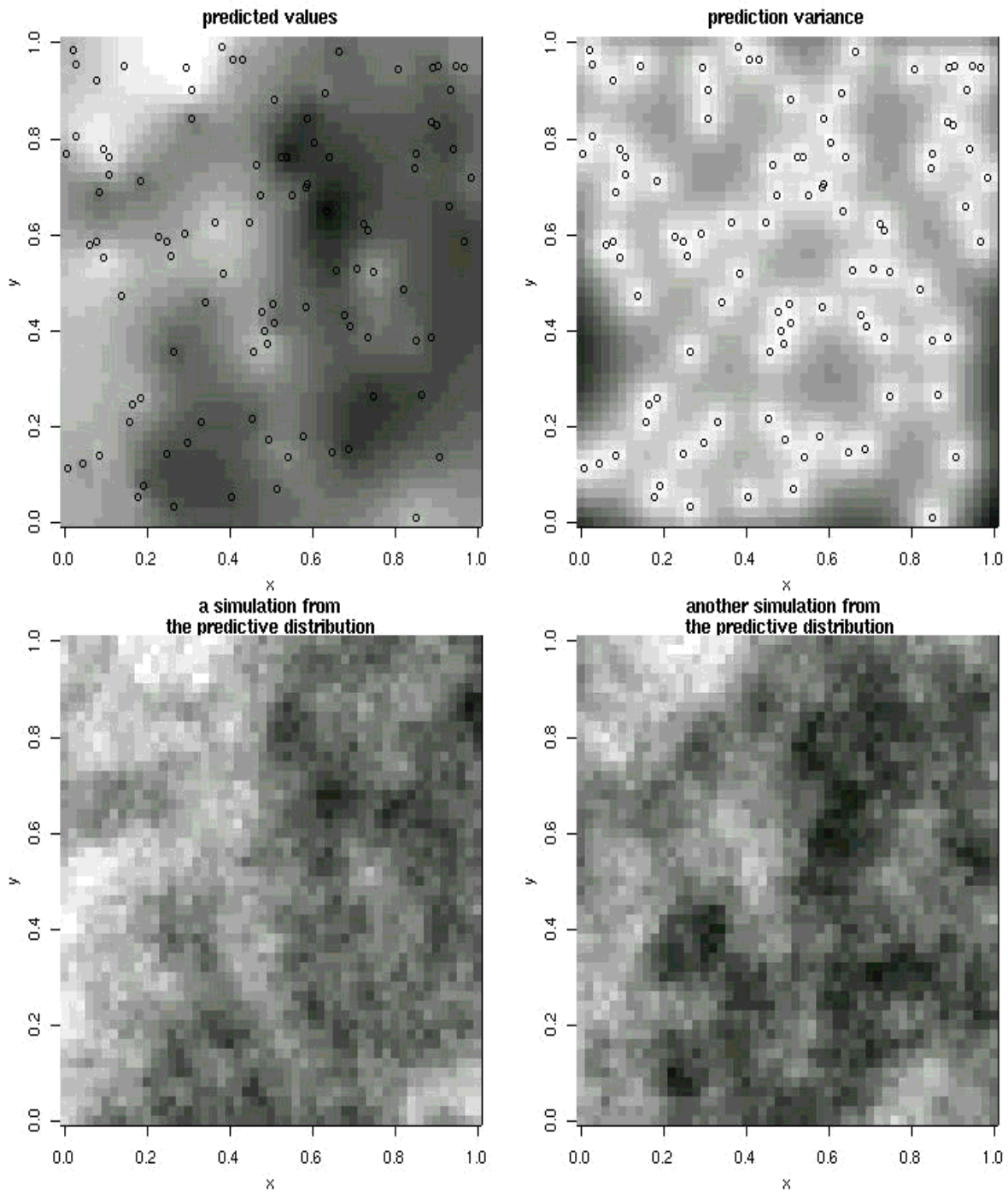
Consider now, under the same model assumptions, obtaining simulations from the predictive distributions on a grid of points covering the area. The commands to define the grid and perform Bayesian prediction are:

```
# definig grid > pred.grid <- expand.grid(seq(0,1, l=101), seq(0,1, l=101))
# Bayesian prediction > bsp <- krige.bayes(s100, loc = pred.grid, prior =
prior.control(range.discrete = seq(0,5,l=251)),
output=output.control(n.predictive=2))
```

## **WARNING: RUNNING THIS COMMAND CAN BE TIME CONSUMING**

Maps with the summaries and simulations of the predictive distribution can be plotted as follows.

```
> par(mfrow=c(2,2))
> image.krige.bayes(bsp, loc = pred.grid, main = "predicted values")
> image.krige.bayes(bsp, val = "moments.variance", loc = pred.grid, main =
"prediction variance")
> image.krige.bayes(bsp, val = "simulation", number.col = 1, loc =
pred.grid, main = "a simulation from\nthe predictive distribution")
> image.krige.bayes(bsp, val = "simulation", number.col = 2, loc =
pred.grid, main = "another simulation from \n the predictive distribution")
```



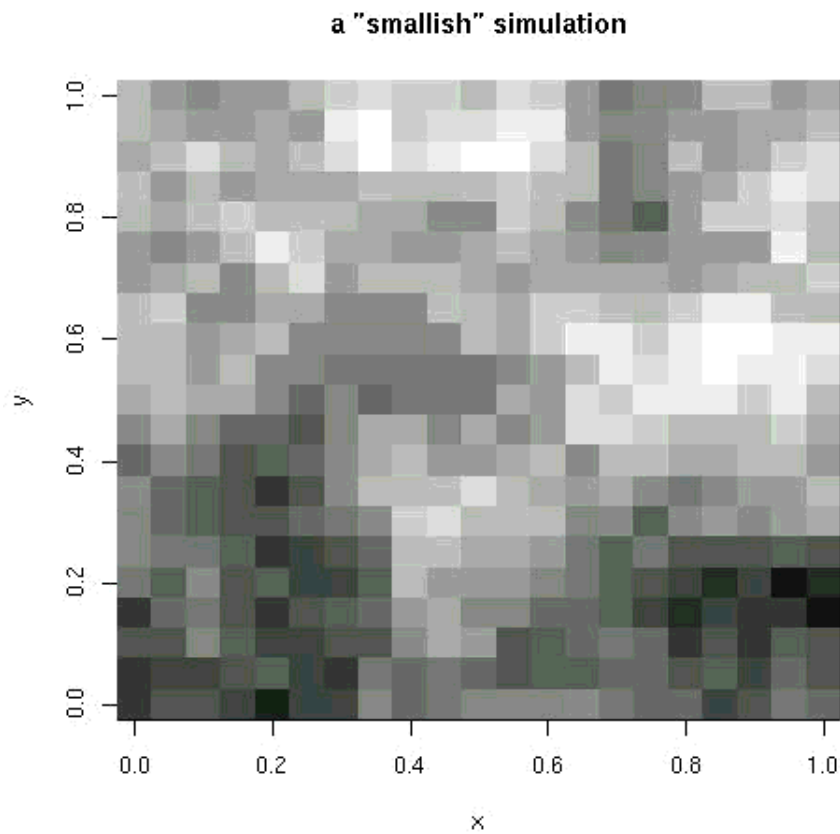
## 6. Simulation of Gaussian Random Fields

The function `grf` generates simulations of Gaussian random fields on regular or irregular sets of locations. Some of its functionality is illustrated by the next commands.

```
> sim1 <- grf(100, cov.pars=c(1, .25))
> points.geodata(sim1, main="simulated locations and values")
> plot(sim1, max.dist=1, main="true and empirical variograms")
```

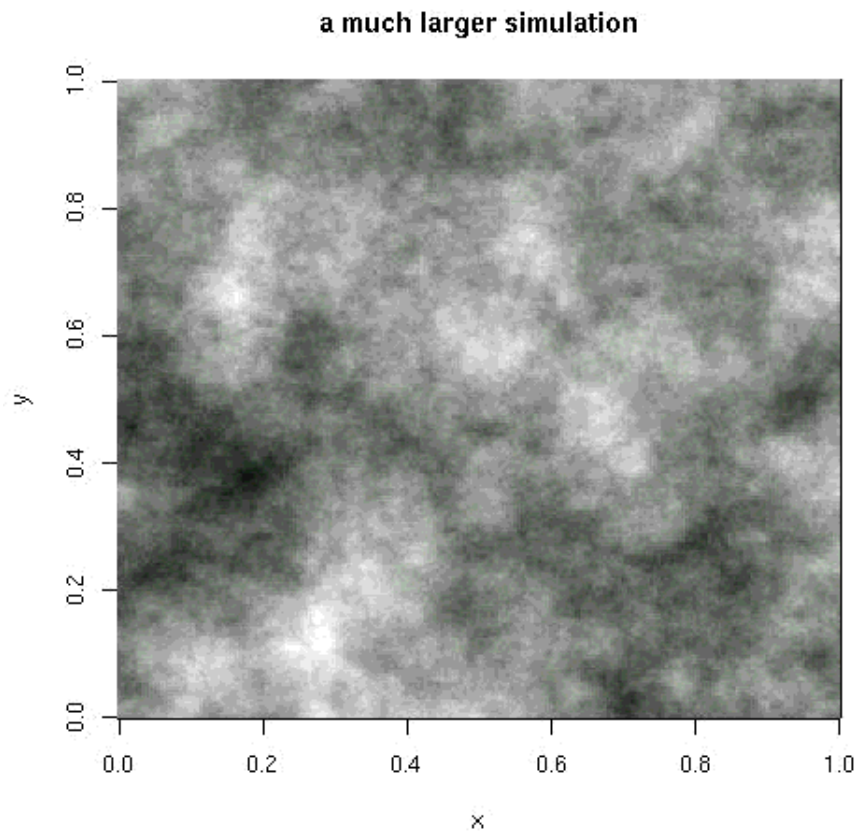


```
> sim2 <- grf(441, grid="reg", cov.pars=c(1, .25))
> image.grf(sim2, main="a \"smallish\" simulation", col=gray(seq(1, .1,
l=30)))
```





```
> sim3 <- grf(40401, grid="reg", cov.pars=c(10, .2), met="circ")  
> image.grf(sim3, main="a much finer grid for the simulation",  
col=gray(seq(1, .1, l=30)))
```



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