The geoR package

Documentation

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R topics documented:

`as.geodata`	*Converts an Object to the Class "geodata"*

Description

Converts a matrix or a data-frame to an object of the `class "geodata"`. Objects of the class `"geodata"` are lists with two obligatory components, `coords` and `data`. Optional components are allowed and a typical example is a vector or matrix with with values of the covariate(s).

Usage

```
as.geodata(obj, coords.col = 1:2, data.col = 3, data.names = NULL,
           covar.col = NULL, covar.names = "obj.names")
```

Arguments

`obj`	a matrix or data-frame. Each line corresponds to one spatial location. It should contain values of coordinates, data and, optionally, covariates at the locations.
`coords.col`	a vector with the column numbers corresponding to the spatial coordinates.
`data.col`	a scalar or vector with column number(s) corresponding to the data.
`data.names`	a string or vector of strings with names for the data columns. Only valid if there is more than one column of data. By default, the names in the original object are used.
`covar.col`	optional. A scalar or vector of the column number(s) corresponding to the covariate(s).
`covar.names`	a string or vector of strings with the name(s) of the covariates. By default, the names in the original object are used.

Details

Objects of the class `"geodata"` contain data for geostatistical analysis using the package **geoR**. Storing data in this format facilitates the usage of the functions in **geoR**. However, conversion of objects to this class is not obligatory to carry out the analysis.

Value

An object of the `class "geodata"` which is a list with two obligatory and one optional component:

`coords`	an $n \times 2$ matrix where n is the number of spatial locations.
`data`	a vector of length n, for the univariate case or, an $n \times v$ matrix or data-frame for the multivariate case, where v is the number of variables.
`covariate`	a vector of length n or an $n \times p$ matrix with covariate(s) values, where p is the number of covariates.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`read.geodata` for reading data from an *ASCII* file and `list` for general information on lists.

`coords.aniso`	*Geometric Anisotropy Correction*

Description

Transforms or back-transforms a set of coordinates according to the geometric anisotropy parameters.

Usage

```
coords.aniso(coords, aniso.pars, reverse = FALSE)
```

Arguments

`coords`	an $n \times 2$ matrix with the coordinates to be transformed.
`aniso.pars`	a vector with two elements, ψ_A and ψ_R, the *anisotropy angle* and the *anisotropy ratio*, respectively. Notice that the parameters must be provided in this order. See section `DETAILS` below for more information on anisotropy parameters.
`reverse`	logical. Defaults to `FALSE`. If `TRUE` the reverse transformation is performed.

Details

Geometric anisotropy is defined by two parameters:

Anisotropy angle defined here as the azimuth angle of the direction with greater spatial continuity, i.e. the angle between the *y-axis* and the direction with the maximum range.

Anisotropy ratio defined here as the ratio between the ranges of the directions with greater and smaller continuity, i.e. the ratio between maximum and minimum ranges. Therefore, its value is always greater or equal to one.

If `reverse = FALSE` (the default) the coordinates are transformed from the *anisotropic space* to the *isotropic space*. The transformation consists in multiplying the original coordinates by a rotation matrix R and a shrinking matrix T, as follows:

$$X_m = XRT,$$

where X_m is a matrix with the modified coordinates (isotropic space) , X is a matrix with original coordinates (anisotropic space), R rotates coordinates according to the anisotropy angle ψ_A and T shrinks the coordinates according to the anisotropy ratio ψ_R.

If `reverse = TRUE`, the back-transformation is performed, i.e. transforming the coordinates from the *isotropic space* to the *anisotropic space* by computing:

$$X = X_m (RT)^{-1}$$

Value

An $n \times 2$ matrix with the transformed coordinates.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

Examples

```
par.mf <- par()$mfrow
par(mfrow=c(3,2))
par(mar=c(2.5,0,0,0))
par(mgp=c(2,.5,0))
par(pty="s")
## Defining a set of coordinates
coords <- expand.grid(seq(-1, 1, l=3), seq(-1, 1, l=5))
plot(c(-1.5, 1.5), c(-1.5, 1.5), xlab="", ylab="", type="n")
text(coords[,1], coords[,2], 1:nrow(coords))
## Transforming coordinates according to some anisotropy parameters
coordsA <- coords.aniso(coords, aniso.pars=c(0, 2))
plot(c(-1.5, 1.5), c(-1.5, 1.5), xlab="", ylab="", type="n")
text(coordsA[,1], coordsA[,2], 1:nrow(coords))
##
coordsB <- coords.aniso(coords, aniso.pars=c(pi/2, 2))
plot(c(-1.5, 1.5), c(-1.5, 1.5), xlab="", ylab="", type="n")
text(coordsB[,1], coordsB[,2], 1:nrow(coords))
##
coordsC <- coords.aniso(coords, aniso.pars=c(pi/4, 2))
plot(c(-1.5, 1.5), c(-1.5, 1.5), xlab="", ylab="", type="n")
text(coordsC[,1], coordsC[,2], 1:nrow(coords))
##
coordsD <- coords.aniso(coords, aniso.pars=c(3*pi/4, 2))
plot(c(-1.5, 1.5), c(-1.5, 1.5), xlab="", ylab="", type="n")
text(coordsD[,1], coordsD[,2], 1:nrow(coords))
##
coordsE <- coords.aniso(coords, aniso.pars=c(0, 5))
plot(c(-1.5, 1.5), c(-1.5, 1.5), xlab="", ylab="", type="n")
text(coordsE[,1], coordsE[,2], 1:nrow(coords))
##
par(mfrow=par.mf)
```

---

cov.spatial   *Computes Value of the Covariance Function*

Description

Computes the covariances for pairs variables, given the separation distance of their locations. Options for different correlation functions are available. The results can be seen as a change of metric, from the *Euclidean distances* to *covariances*.

Usage

```
cov.spatial(obj, cov.model=c("exponential", "matern", "gaussian",
            "spherical", "circular", "cubic", "wave",
            "powered.exponential", "cauchy",
            "gneiting", "gneiting.matern", "pure.nugget"),
            cov.pars=stop("no cov.pars argument provided"), kappa)
```

Arguments

obj
: a numeric object (vector or matrix), typically with values of distances between pairs of spatial locations.

cov.model
: a string indicating the type of the correlation function. See section DETAILS for available options and expressions of the correlation functions.

cov.pars
: a vector with 2 elements or an $ns \times 2$ matrix with the covariance parameters. The first element (if a vector) or first column (if a matrix) corresponds to the variance parameter σ^2. The second element or column corresponds to the range parameter ϕ of the correlation function. If a matrix is provided, each row corresponds to the parameters of one *spatial structure*. Models with several structures are also called *nested models* in the geostatistical literature.

kappa
: numerical value for the additional smoothness parameter of the correlation function. Only required by the following correlation functions: "matern", "powered.exponential", "gneiting" and "gneiting.matern".

Details

Covariance functions return the value of the covariance $C(h)$ between a pair variables located at points separated by the distance h. The covariance function can be written as a product of a variance parameter σ^2 times a positive definite *correlation function* $\rho(h)$:

$$C(h) = \sigma^2 \rho(h).$$

The expressions of the covariance functions available in **geoR** are given below. We recommend the *LaTeX* (and/or the corresponding *.dvi, .pdf* or *.ps*) version of this document for better visualization of the formulas.

Denote ϕ the basic parameter of the correlation function and name it the *range parameter*. Some of the correlation functions will have an extra parameter κ, the *smoothness parameter*. $K_\kappa(x)$ denotes the modified Bessel function of the third kind of order κ. See documentation of the function besselK for further details. In the equations below the functions are valid for $\phi > 0$ and $\kappa > 0$, unless stated otherwise.

exponential

$$\rho(h) = \exp(-\frac{h}{\phi})$$

wave

$$\rho(h) = \frac{\phi}{h}\sin(\frac{h}{\phi})$$

matern

$$\rho(h) = \frac{1}{2^{\kappa-1}\Gamma(\kappa)}(\frac{h}{\phi})^{\kappa}K_{\kappa}(\frac{h}{\phi})$$

gaussian

$$\rho(h) = \exp[(-\frac{h}{\phi})^2]$$

spherical

$$\rho(h) = \begin{cases} 1 - 1.5\frac{h}{\phi} + 0.5(\frac{h}{\phi})^3 & \text{, if } h < \phi \\ 0 & \text{, otherwise} \end{cases}$$

circular
Let $\theta = \min(\frac{h}{\phi}, 1)$ and

$$g(h) = 2\frac{(\theta\sqrt{1-\theta^2} + \sin^{-1}\sqrt{\theta})}{\pi}.$$

Then, the circular model is given by:

$$\rho(h) = \begin{cases} 1 - g(h) & \text{, if } h < \phi \\ 0 & \text{, otherwise} \end{cases}$$

cubic

$$\rho(h) = \begin{cases} 7(\frac{h}{\phi})^2 - 8.75(\frac{h}{\phi})^3 + 3.5(\frac{h}{\phi})^5 - 0.75(\frac{h}{\phi})^7 & \text{, if } h < \phi \\ 0 & \text{, otherwise} \end{cases}$$

powered.exponential

$$\rho(h) = \exp[-(\frac{h}{\phi})^{\kappa}] \ , \ 0 < \kappa \le 2$$

cauchy

$$\rho(h) = [1 + (\frac{h}{\phi})^2]^{-\kappa}$$

gneiting
Let $\theta = \min(\frac{h}{\phi}, 1)$. The Gneiting model is given by:

$$\rho(h) = (1 + 8\theta + 25\theta^2 + 32\theta^3)(1 - \theta)^8$$

gneiting.matern
Let $\alpha = \phi\kappa_2$, $\rho_m(\cdot)$ denotes the Matérn model and $\rho_g(\cdot)$ the Gneiting model. Then the Gneiting-Matérn is given by

$$\rho(h) = \rho_g(h|\phi = \alpha)\,\rho_m(h|\phi = \phi, \kappa = \kappa_1)$$

Value

The function returns values of the covariances corresponding to the given distances. The type of output is the same as the type of the object provided in the argument `obj`, typically a vector, matrix or array.

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References

For a review on correlation functions:
Schlather, M. (1999) *An introduction to positive definite functions and to unconditional simulation of random fields*. Technical report ST 99-10, Dept. of Maths and Statistics, Lancaster University.

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`matern` for computation of the Matérn model, `besselK` for computation of the Bessel function and `varcov.spatial` for computations related to the covariance matrix.

Examples

```
#
# Variogram models with the same "practical" range:
#
xval <- seq(0,1,l=101)
vexp <- cov.spatial(xval, cov.pars=c(1, .2))
vsph <- cov.spatial(xval, cov.pars=c(1, .60), cov.model="sph")
vgau <- cov.spatial(xval, cov.pars=c(1, .60/sqrt(3)),
                    cov.model="gau")
plot(0:1, 0:1, type="n", xlab="distance",
     ylab=expression(gamma(h)),
     main="variograms with equivalent \"practical range\"")
lines(xval, (1-vexp))
lines(xval, (1-vsph), lty=2)
lines(xval, (1-vgau), lwd=2)
legend(0.5,.3, c("exponential", "spherical", "gaussian"),
       lty=c(1,2,1), lwd=c(1,1,2))
#
# Matern models with equivalent "practical range"
# and varying smoothness parameter
#
dval <- seq(0,1,l=101)
mat.5 <- cov.spatial(dval, cov.pars = c(1, 0.25), kappa = 0.5)
mat1 <-  cov.spatial(dval, cov.pars = c(1, 0.188), kappa = 1,
                     cov.model="mat")
mat2 <-  cov.spatial(dval, cov.pars = c(1, 0.14), kappa = 2,
                     cov.model="mat")
mat3 <-  cov.spatial(dval, cov.pars = c(1, 0.117), kappa = 3,
                     cov.model="mat")
plot(0:1, 0:1, type="n", xlab="distance",
```

```
        ylab=expression(gamma(h)),
        main="models with equivalent \"practical\" range")
lines(dval, 1-mat.5, lty=2)
lines(dval, 1-mat1)
lines(dval, 1-mat2, lwd=2, lty=2)
lines(dval, 1-mat3, lwd=2)
legend(0.5,.3, c(expression(paste(kappa == 0.5, "  and  ",
        phi == 0.250)),
expression(paste(kappa == 1, "  and  ", phi == 0.188)),
expression(paste(kappa == 2, "  and  ", phi == 0.140)),
expression(paste(kappa == 3, "  and  ", phi == 0.117))),
lty=c(2,1,2,1), lwd=c(1,1,2,2))
```

---

grf   *Simulation of Gaussian Random Fields*

Description

Generates simulations of Gaussian random fields for given covariance parameters.

Usage

```
grf(n, grid = "irreg", nx = round(sqrt(n)), ny = round(sqrt(n)),
    xlims = c(0, 1), ylims = c(0, 1), nsim = 1,
    cov.model = c("exponential", "matern", "gaussian",
                  "spherical", "circular", "cubic", "wave",
                  "powered.exponential", "cauchy", "gneiting",
                  "gneiting.matern", "pure.nugget"),
    cov.pars = stop("cov. parameters (sigmasq and phi) needed"),
    kappa = 0.5, nugget = 0, lambda = 1, aniso.pars,
    method = c("cholesky", "svd", "eigen", "circular.embedding"),
    messages.screen = TRUE)
```

Arguments

n	number of points (spatial locations) in each simulations.
grid	optional. An $n \times 2$ matrix with coordinates of the simulated data.
nx	optional. Number of points in the X direction.
ny	optional. Number of points in the X direction.
xlims	optional. Limits of the area in the X direction. Defaults to $[0, 1]$.
ylims	optional. Limits of the area in the Y direction. Defaults to $[0, 1]$.
nsim	Number of simulations. Defaults to 1.
cov.model	correlation function. See cov.spatial for further details. Defaults to "exponential".
cov.pars	a vector with 2 elements or an $n \times 2$ matrix with values of the covariance parameters σ^2 (partial sill) and ϕ (range parameter). If a vector, the elements are the values of σ^2 and ϕ, respectively. If a matrix, corresponding to a model with several structures, the values of σ^2 are in the first column and the values of ϕ are in the second.

kappa	additional smoothness parameter required only for the following correlation functions: `"matern"`, `"powered.exponential"`, `"gneiting"` and `"gneiting.matern"`. More details on the documentation for the function `cov.spatial`.
nugget	the value of the nugget effect parameter τ^2.
lambda	value of the Box-Cox transformation parameter. The value $\lambda = 1$ corresponds to no transformation, the default. For any other value of λ Gaussian data is simulated and then transformed.
aniso.pars	geometric anisotropy parameters. By default an isotropic field is assumed and this argument is ignored. If a vector with 2 values is provided, with values for the anisotropy angle ψ_A (in radians) and anisotropy ratio ψ_A, the coordinates are transformed, the simulation is performed on the isotropic (transformed) space and then the coordinates are back-transformed such that the resulting field is anisotropic. Coordinates transformation is performed by the function `coords.aniso`.
method	simulation method. Defaults to the *Cholesky* decomposition. See section `DETAILS` below.
messages.screen	
	logical, indicating whether or not status messages are printed on the screen (or output device) while the function is running. Defaults to `TRUE`.

Details

For the methods `"cholesky"`, `"svd"` and `"eigen"` the simulation consists of multiplying a vector of standardized normal deviates by a square root of the covariance matrix. The square root of a matrix is not uniquely defined. The three available methods differs in the way they compute the square root of the (positive definite) covariance matrix.

For `method = "circular.embedding"` the algorithm implements the method described by Wood & Chan (1994) which is based on Fourier transforms. Only regular and equally spaced grids can be generated using this method.
The code for the `"circular.embedding"` method was provided by Martin Schlather, University of Bayreuth
(`http://btgyn8.geo.uni-bayreuth.de/~martin/`).

WARNING: The code for the `"circular.embedding"` method is no longer being maintained. Martin will soon release a package for unconditional simulation of random fields. This will be announced on the R (contributed packages) and **geoR** home page. When this new package is released the current implementation of the `"circular.embedding"` method might become obsolete.

Value

A list with the components:

coords	an $n \times 2$ matrix with the coordinates of the simulated data.
data	a vector (if `nsim = 1`) or a matrix with the simulated values. For the latter each column corresponds to one simulation.
cov.model	a string with the name of the correlation.
nugget	the value of the nugget parameter.
cov.pars	a vector with the values of σ^2 and ϕ, respectively.
kappa	value of the parameter κ.

`lambda`	value of the Box-Cox transformation parameter λ.
`aniso.pars`	a vector with values of the anisotropy parameters, if provided in the function call.
`method`	a string with the name of the simulation method used.
`.Random.seed`	the random seed at the time the function was called.
`messages`	messages produced by the function describing the simulation.
`call`	the function call.

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References

Wood, A.T.A. and Chan, G. (1994) Simulation of stationary Gaussian process in $[0, 1]^d$. *Journal of Computatinal and Graphical Statistics*, **3**, 409–432.

Schlather, M. (1999) *Introduction to positive definite functions and to unconditional simulation of random fields*. Tech. Report ST–99–10, Dept Maths and Stats, Lancaster University.

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`plot.grf` and `image.grf` for graphical output, `coords.aniso` for anisotropy coordinates transformation and, `chol`, `svd` and `eigen` for methods of matrix decomposition.

Examples

```
sim1 <- grf(100, cov.pars=c(1, .25))
# a display of simulated locations and values
points.geodata(sim1)
# empirical and theoretical variograms
plot(sim1)
#
# a "smallish" simulation
sim2 <- grf(441, grid="reg", cov.pars=c(1, .25))
image.grf(sim2)
#
# a "bigger" one
sim3 <- grf(40401, grid="reg", cov.pars=c(10, .2), met="circ")
image.grf(sim3)
```

| image.grf | *Image or Perspective Plot of Simulated Gaussian Random Field* |

Description

Plots an image or perspective plot with a realization of a Gaussian random field, simulated using the function grf.

Usage

```
image.grf(obj, sim.number = 1, ...)

persp.grf(obj, sim.number = 1, ...)
```

Arguments

obj	an object of the class grf, typically an output of the function grf.
sim.number	simulation number. Indicates the number of the simulation top be plotted. Only valid if the object contains more than one simulation. Defaults to 1.
...	further arguments to be passed to the functions image or persp.

Value

An image or perspective plot is produced on the current graphics device. No values are returned.

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

grf for simulation of Gaussian random fields, image and persp for the generic plotting functions.

Examples

```
# generating 4 simulations of a Gaussian random field
sim <- grf(225, grid="reg", cov.pars=c(1, .25), nsim=4)
par.ori <- par()
par(mfrow=c(2,2))
par(pty="s")
for (i in 1:4)
  image.grf(sim, sim.n=i)
```

`image.krige.bayes`   *Plots Results of the Predictive Distribution*

Description

This function produces an image or perspective plot of a selected element of the predictive distribution returned by the function `krige.bayes`.

Usage

```
image.krige.bayes(obj, locations,
          values.to.plot=c("moments.mean", "moments.variance",
                    "mean.simulations", "variance.simulations",
                    "quantiles", "probability", "simulation"),
          number.col, ...)

persp.krige.bayes(obj, locations,
          values.to.plot=c("moments.mean", "moments.variance",
                    "mean.simulations", "variance.simulations",
                     "quantiles", "probability", "simulation"),
          number.col, ...)
```

Arguments

`obj`	an object of the class `krige.bayes`, typically an output of the function `krige.bayes`.
`locations`	an $n \times 2$ matrix with the coordinates of the prediction locations, which should define a regular grid in order to be plotted by `image` or `persp`.
`values.to.plot`	select the element of the predictive distribution to be plotted. See DETAILS below.
`number.col`	Specifies the number of the column to be plotted. Only used if `values.to.plot` is set to one of `"quantile"`, `"probability"` or `"simulation"`.
`coords.data`	optional. If an $n \times 2$ matrix with the data coordinates is provided, points indicating the data locations are included in the plot.
`...`	extra arguments to be passed to the plotting function `image` or `persp`.

Details

The function `krige.bayes` returns summaries and other results about the predictive distributions. The argument `values.to.plot` specifies which result will be plotted. It can be passed to the function in two different forms:

- a vector with the object containing the values to be plotted, or
- one of the following options: `"moments.mean"`, `"moments.variance"`, `"mean.simulations"`, `"variance.simulations"`, `"quantiles"`, `"probability"` or `"simulation"`.

For the last three options, if the results are stored in matrices, a column number must be provided using the argument `number.col`.

The documentation for the function `krige.bayes` provides further details about these options.

Value

An `image` or `persp` plot is produced on the current graphics device. No values are returned.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`krige.bayes` for Bayesian Kriging computations and, `image` and `persp` for the generic plotting functions.

Examples

```
#See examples in the documentation for the function krige.bayes().
```

---

image.kriging	*Image or Perspective Plot with Kriging Results*

Description

Plots image or perspective plots with results of the kriging calculations.

Usage

```
image.kriging(kriging.obj, location = kriging.obj$locations,
              values = kriging.obj$predict, ...)

persp.kriging(kriging.obj, locations=kriging.obj$locations,
              values=kriging.obj$predict, ...)
```

Arguments

kriging.obj   an object of the class `kriging`, typically with the output of the functions `krige.conv` or `ksline`.

locations   an $n \times 2$ matrix with the coordinates of the prediction locations, which should define a regular grid in order to be plotted by `image` or `persp`.

values   a vector with values to be plotted. Defaults to `obj$predict`.

coords.data   optional. If an $n \times 2$ matrix with the data coordinates is provided, points indicating the data locations are included in the plot.

...   further arguments to be passed to the functions `image` or `persp`.

Value

An image or perspective plot is produced o the current graphics device. No values are returned.

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`krige.conv` and `ksline` for kriging calculations. Documentation for `image` and `persp` contain basic information on the plotting functions.

Examples

```
if(is.R()) data(s100)
loci <- expand.grid(seq(0,1,l=31), seq(0,1,l=31))
kc <- krige.conv(s100, loc=loci,
                 krige=krige.control(cov.pars=c(1, .25)))
par(mfrow=c(1,2))
image.kriging(kc, loc=loci)
image.kriging(kc, loc=loci, val=kc$krige.var)
```

`krige.bayes`	*Bayesian Analysis for Gaussian Geostatistical Models*

Description

The function `krige.bayes` performs Bayesian analysis of geostatistical data allowing specifications of different levels of uncertainty in the model parameters.
It returns results on the posterior distributions for the model parameters and on the predictive distributions for prediction locations (if provided).

Usage

```
krige.bayes(geodata, coords = geodata$coords, data = geodata$data,
            locations = "no",
      model = model.control(trend.d = "cte", trend.l = "cte",
                    cov.model = "exponential", kappa = 0.5,
                    aniso.pars = NULL, lambda = 1),
      prior = prior.control(beta.prior = c("flat", "normal",
                                           "fixed"),
                    beta = NULL, beta.var = NULL,
                    sill.prior = c("reciprocal", "fixed"),
                    sill = NULL,
```

```
                      range.prior = c("uniform", "exponential",
                                      "fixed", "squared.reciprocal",
                                      "reciprocal"),
                      exponential.prior.par = 1, range = NULL,
                      range.discrete = NULL,
                      nugget.prior = c("fixed", "uniform"),
                      nugget = 0, nugget.discrete = NULL),
         output = output.control(n.posterior = 1000,
                      n.predictive = NULL, moments = TRUE,
                      simulations.predictive = TRUE,
                      keep.simulations = TRUE, mean.estimator = TRUE,
                      quantile.estimator =  NULL,
                      probability.estimator = NULL,
                      signal = FALSE, messages.screen = TRUE))
```

Arguments

geodata   a list containing elements `coords` and `data` as described next. Typically
             an object of the class `"geodata"` - a **geoR** data-set. If not provided the
             arguments `coords` and `data` must be provided instead.

coords   an $n \times 2$ matrix where each row has the 2-D coordinates of the n data
             locations. By default it takes the component `coords` of the argument
             `geodata`, if provided.

data   a vector with n data values. By default it takes the component `data` of
             the argument `geodata`, if provided.

locations   an $N \times 2$ matrix or data-frame with the 2-D coordinates of the N predic-
             tion locations. Defaults to `"no"` in which case the function returns only
             results on the posterior distributions of the model parameters.

model   defines model components. See section DETAILS below.

prior   specification of priors for the model parameters. See section DETAILS
             below.

output   Defines output options. See section DETAILS below.

Details

`krige.bayes` is a generic function for Bayesian geostatistical analysis where predictions can
take into account the parameter uncertainty.

It can be set to run conventional kriging methods which use known parameters or *plug-in*
estimates. However, the functions `krige.conv` and `ksline` are preferable for prediction
with fixed parameters.

The basis for the Bayesian algorithm is to discretize the prior distribution for the param-
eters ϕ and $\tau^2_{rel} = \frac{\tau^2}{\sigma^2}$. The Tech. Report referenced below provides details on the results
used in the current implementation.

CONTROL FUNCTIONS

The function call includes auxiliary control functions which allows the user to specify
and/or change the specification of model components (using `model.control`), prior
distributions (using `prior.control`) and output options (using `output.control`). Default
options are available in most of the cases. The arguments for the control functions are as

follows.

ARGUMENTS FOR CONTROL FUNCTIONS

Arguments for `model = model.control(...)` :

trend.d specifies the trend (covariates) values at the data locations. Possible values are: `"cte"` - model with constant mean, `"1st"` - trend is defined as a first degree polynomial on the coordinates, `"2nd"` - trend is defined as a second degree polynomial on the coordinates, a formula of the type `~X`, where `X` is a matrix with covariates (external trend) at data locations. Defaults to `"cte"`.

trend.l specifies the trend (covariates) at the prediction locations. Must be of the same type as defined for `trend.d`. Only used if prediction locations are provided in the argument `locations`.

cov.model string indicating the name of the model for the correlation function. Further details in the documentation for `cov.spatial`.

kappa additional smoothness parameter. Only used if the correlation function is one of: `"matern"`, `"powered.exponential"`, `"gneiting"` or `"gneiting.matern"`. In the current implementation this parameter is always regarded as fixed during the Bayesian analysis.

aniso.pars fixed parameters for geometric anisotropy correction. If `aniso.pars = FALSE` no correction is made, otherwise a two elements vector with values for the anisotropy parameters must be provided. Anisotropy correction consists of a transformation of the data and prediction coordinates performed by the function `coords.aniso`.

lambda numerical value of the Box-Cox transformation parameter. The value $\lambda = 1$ corresponds to no transformation. The Box-Cox parameter λ is always regarded as fixed and data transformation is performed before the analysis. Prediction results are back-transformed and returned is the same scale as for the original data. For $\lambda = 0$ the log-transformation is performed. If $\lambda < 0$ the mean predictor doesn't make sense (the resulting distribution has no expectation).

Arguments for `output = output.control(...)` :

n.posterior number of samples to be taken from the posterior distribution.

n.predictive number of samples to be taken from the predictive distribution. By default equals to `n.posterior`.

moments logical. If `TRUE` moments of the predictive distribution are computed analytically (without sampling). Valid only if `lambda = 1` or `lambda = 0`.

simulations.predictive logical. Defines whether simulations are drawn from the predictive distribution. Only valid if prediction locations are provided on the argument `locations`.

keep.simulations logical. Indicates whether or not the samples of the predictive distributions are returned. Only valid if prediction locations are provided on the argument `locations`.

mean.estimator logical. Indicates whether or not the mean and variances of the predictive distributions are computed and returned. If `TRUE` the objects `predict.mean` and `krige.var` are included in the output. Only valid if prediction locations are provided on the argument `locations`.

quantile.estimator indicates whether or not quantiles of the predictive distributions are computed and returned. If a vector with numbers in the interval $[0, 1]$ is provided the output includes the object `quantiles`, which contains values of corresponding estimated quantiles. For example, if `estimator = c(0.25,0.50,0.75)` the function returns the quartiles of the distributions at each of the prediction locations. If `quantile.estimator = TRUE`, the default, the vector `c(0.025, 0.5, 0.975)`, is assumed. A measure of uncertainty for the predictions, which is analogous to the kriging standard error, can be computed by $(quantile0.975 - quantile0.025)/4$. Only used if prediction locations are provided in the argument `locations`.

probability.estimator the default is `FALSE` for which case nothing is computed. If some cutoff values are provided instead, an object called `probability` is included in the output. This object contains, for each prediction location, the probability that the variable is less than or equal to the cutoff value given in the argument.

signal logical. If `TRUE` the signal is predicted, otherwise the variable is predicted. If no transformation is performed the expectations are the same in both cases and the kriging variances are different, if the nugget is different of zero.

messages.screen logical. Indicates whether or not status messages are printed on the screen (or output other device) while the function is running.

Value

An object of the `class "krige.bayes"` which is a list with the following components:

`posterior`	A list with results for the posterior distribution of the model parameters. The components are:
`beta.summary`	summary for the posterior distribution of the mean parameter β.
`sigmasq.summary`	
	summary for the posterior distribution of the variance parameter σ^2 (partial sill).
`phi.summary`	summary for the posterior distribution of the correlation parameter ϕ (range parameter) .
`tausq.summary`	summary for the posterior distribution of the nugget variance parameter τ^2.
`beta.samples`	samples from the posterior distribution of the mean parameter β.
`sigmasq.samples`	
	samples from the posterior distribution of the variance parameter σ^2.
`phi.samples`	samples from the posterior distribution of the correlation parameter ϕ.
`tausq.samples`	samples from the posterior distribution of the nugget variance parameter τ^2.
`phi.marginal`	samples from the marginal posterior distribution of the correlation parameter ϕ, resulting from averaging the posterior over the distribution of (β, σ^2).
`nugget.marginal`	
	samples from the marginal posterior distribution of the nugget variance parameter τ^2, resulting from averaging the posterior over the distribution of (β, σ^2).
`predictive`	A list with results for the predictive distribution of the prediction locations (if provided). The components are:

`moments`   a numerical matrix. The columns contains the estimated moments of the predictive distribution, at each prediction location

`simulations`   a numerical matrix. Each column has a simulation from the predictive distribution. Returned only if `keep.simulations = TRUE`.

`mean.simulations`

a vector with the estimated mean at the prediction locations computed by averaging over the simulations. Returned only if `mean.estimator = TRUE`.

`variance.simulations`

a vector with the estimated variance at the prediction locations, computed using the simulations. Returned only if `mean.estimator = TRUE`.

`quantile`   A matrix or vector with quantile estimators. Returned only if the argument `quantile.estimator` is used.

`probability`   A matrix or vector with probability estimators. Returned only if the argument `probability.estimator` is used.

`type.prediction`

information on the type of prediction performed.

`message.prediction`

information about the parameter uncertainty taken into account. Indicates which parameters has been regarded as random during the analysis.

`.Random.seed`   system random seed before running the function. Allows reproduction of results. If the `.Random.seed` is set to this value and the function is run again, it will produce exactly the same results.

`call`   the function call.

Auxiliary functions

The functions of type `krige.bayes.aux` and `control` are auxiliary functions called by `krige.bayes`.

Author(s)

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References

The technical details about the implementation of `krige.bayes` can be found at:

Ribeiro, P.J. Jr. and Diggle, P.J. (1999) *Bayesian inference in Gaussian model-based geostatistics.* Tech. Report ST-99-08, Dept Maths and Stats, Lancaster University.
Available at:
http://www.maths.lancs.ac.uk/~ribeiro/publications.html

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`lines.krige.bayes`, `image.krige.bayes` and `persp.krige.bayes` for graphical output of the results. `krige.conv` and `ksline` for conventional kriging methods.

Examples

```
# generating a simulated data-set
ex.data <- grf(50, cov.pars=c(10, .25))
#
# defining the prediction grid:
ex.grid <- as.matrix(expand.grid(seq(0,1,l=11), seq(0,1,l=11)))
#
# computing Bayesian posterior and predictive distributions



ex.bayes <- krige.bayes(ex.data, loc=ex.grid, prior =
                 prior.control(range.discrete=seq(0, 2, l=51)))

#
# Ploting theoretical amd empirical variograms
plot(ex.data)
# adding lines with fitted variograms
lines(ex.bayes, max.dist=1.2)
lines(ex.bayes, max.dist=1.2, summ="median", lty=2)
lines(ex.bayes, max.dist=1.2, summ="mean", lwd=2, lty=2)
#
# Ploting prediction some results
par.mf <- par()$mfrow
par(mfrow=c(2,2))
image.krige.bayes(ex.bayes, loc=ex.grid, main="predicted values")
image.krige.bayes(ex.bayes, val="moments.variance",
                  loc=ex.grid, main="prediction variance")
image.krige.bayes(ex.bayes, val= "simulation", number.col=1,
                  loc=ex.grid,
     main="a simulation from the \npredictive distribution")
image.krige.bayes(ex.bayes, val= "simulation", number.col=2,
                  loc=ex.grid,
    main="another simulation from \nthe predictive distribution")
par(mfrow=par.mf)
```

---

krige.conv	*Spatial Prediction – Conventional Kriging*

Description

This function performs spatial prediction for fixed covariance parameters using global neighborhood.

Available options implement the following kriging types: *SK* (simple kriging), *OK* (ordinary kriging), *KTE* (external trend kriging) and *UK* (universal kriging).

Usage

```
krige.conv(geodata, coords = geodata$coords, data = geodata$data,
           locations,
           krige = krige.control(type.krige, beta = NULL,
                     trend.d, trend.l, cov.model, cov.pars,
                     kappa = 0.5, nugget = 0, micro.scale = 0,
```

```
                        dist.epsilon = 1e-10, aniso.pars = NULL,
                        lambda = 1, signal = FALSE,
                        n.samples.backtransform = 500, n.sim = 0),
            messages.screen = TRUE)
```

Arguments

geodata a list containing elements `coords` and `data` as described next. Typically an object of the `class "geodata"` - a **geoR** data-set. If not provided the arguments `coords` and `data` must be provided instead.

coords an $n \times 2$ containing in each row have the 2-D coordinates of the n data locations. By default it takes the component `coords` of the argument `geodata`, if provided.

data a vector with n data values. By default it takes the component `data` of the argument `geodata`, if provided.

locations an $N \times 2$ matrix or data-frame with the 2-D coordinates of the N prediction locations.

krige defines the model components and the type of kriging. See section DE-TAILS below.
ATTENTION: the argument `cov.pars` is obligatory whilst all the others have default options.

messages.screen
logical. Indicates whether or not status messages are printed on the screen (or other output device) while the function is running.

Details

One of the following different types of kriging: *SK, OK, UK* or *KTE* is performed, according to the input options. Defaults correspond to ordinary kriging.

Arguments for `krige = krige.control(...)` :

type.krige type of kriging to be performed. Options are `"SK"`, `"OK"` corresponding to simple or ordinary kriging. Kriging with external trend and universal kriging can be defined setting `type.krige = "OK"` and specifying the trend model using the arguments `trend.d` and `trend.l`.

beta numerical value of the mean (vector) parameter. Only used if `type.krige="SK"`.

trend.d specifies the trend (covariates) values at the data locations. Possible values are: `"cte"` - model with constant mean, i.e. no trend `"1st"` - trend is defined as a first degree polynomial on the coordinates `"2nd"` - trend is defined as a second degree polynomial on the coordinates a formula of the type ~X, where X is a matrix with covariates (external trend) at data locations. Defaults to `"cte"`.

trend.l specifies the trend (covariate) at prediction locations. It must be of the same type as defined in `trend.d`. Only used if prediction locations are provided in the argument `locations`.

cov.model string indicating the name of the model for the correlation function. Further details in the documentation for `cov.spatial`.

cov.pars a vector with 2 elements or an $n \times 2$ matrix with the covariance parameters σ^2 (partial sill) and ϕ (range parameter). If a vector, the elements are the values of σ^2 and ϕ, respectively. If a matrix, corresponding to a model with several structures, the values of σ^2 are in the first column and the values of ϕ are in the second.

kappa additional smoothness parameter required by the following correlation functions: `"matern"`, `"powered.exponential"`, `"gneiting"` and `"gneiting.matern"`.

nugget the value of the nugget variance parameter τ^2. Defaults to zero.

micro.scale micro-scale variance. If different from zero, the nugget variance is divided into 2 terms: *micro-scale variance* and *measurement error*. This might affect the precision of the predictions. In practice, these two variance components are usually indistinguishable but the distinction can be made here if justifiable.

dist.epsilon a numeric value. Points which are separated by a distance less than this value are considered co-located.

aniso.pars parameters for geometric anisotropy correction. If `aniso.pars = FALSE` no correction is made, otherwise a two elements vector with values for the anisotropy parameters must be provided. Anisotropy correction consists of a transformation of the data and prediction coordinates performed by the function `coords.aniso`.

lambda numeric value of the Box-Cox transformation parameter. The value $\lambda = 1$ corresponds to no transformation and $\lambda = 0$ corresponds to the log-transformation. Prediction results are back-transformed and returned is the same scale as for the original data.

signal logical. If `TRUE` the signal is predicted, otherwise the variable is predicted. If no transformation is performed the expectations are the same in both cases and the difference is only for values of the kriging variance, if the value of the nugget is different from zero.

n.samples.backtransform number of samples used in the back-transformation. When transformations are used (specified by an argument `lambda`), back-transformations are usually performed by sampling from the predictive distribution and then back-transforming the sampled values. The exceptions are for $\lambda = 0$ (log-transformation) and $\lambda = 1$ (no transformation).

n.sim optional. Number of simulations from the posterior distribution. If `n.sim` is provided, samples are taken from the predictive distribution. This corresponds to realizations of conditional simulations, given the data.

Value

An object of the `class kriging` which is a list with the following components:

`predict`	a vector with predicted values.
`krige.var`	a vector with predicted variances.
`beta.est`	estimates of the β, parameter implicit in kriging procedure. Not valid if `type.krige = "SK"`.
`simulations`	an $ni \times n.sim$ matrix where ni is the number of prediction locations. Each column corresponds to a conditional simulation of the predictive distribution. Only returned if `n.sim > 0`.
`message`	messages about the type of prediction performed.
`call`	the function call.

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`image.kriging` for graphical output of the results, `krige.bayes` for Bayesian prediction and `ksline` for a different implementation of kriging allowing for moving neighborhood.

Examples

```
if(is.R()) data(s100)
loci <- expand.grid(seq(0,1,l=31), seq(0,1,l=31))
kc <- krige.conv(s100, loc=loci,
                 krige=krige.control(cov.pars=c(1, .25)))
par(mfrow=c(1,2))
image.kriging(kc, loc=loci, main="kriging estimates")
image.kriging(kc, loc=loci, val=sqrt(kc$krige.var),
              main="kriging std. errors")
```

---

ksline	*Spatial Prediction – Conventional Kriging*

Description

This function performs spatial prediction for given covariance parameters. Options implement the following kriging types: *SK* (simple kriging), *OK* (ordinary kriging), *KTE* (external trend kriging) and *UK* (universal kriging).

The function `krige.conv` should be preferred, unless moving neighborhood is to be used.

Usage

```
ksline(geodata, coords = geodata$coords, data = geodata$data,
       locations,
       cov.model = c("exponential", "matern", "gaussian",
                     "spherical", "circular", "cubic", "wave",
                     "powered.exponential", "cauchy", "gneiting",
                     "gneiting.matern", "pure.nugget"),
       cov.pars=stop("cov. parameters (sigmasq and phi) needed"),
       kappa = 0.5, nugget = 0, micro.scale = 0,
       lambda = 1, m0 = "ok", nwin = "full",
       n.samples.backtransform = 500, trend = 1, d = 2,
       ktedata = NULL, ktelocations = NULL, aniso.pars = NULL,
       signal = FALSE, dist.epsilon = 1e-10,
       messages.screen = TRUE)
```

Arguments

geodata	a list containing elements `coords` and `data` as described next. Typically an object of the `class "geodata"` - a **geoR** data-set. If not provided the arguments `coords` and `data` must be provided instead.
coords	an $n \times 2$ matrix where each row has the 2-D coordinates of the n data locations. By default it takes the component `coords` of the argument geodata, if provided.
data	a vector with n data values. By default it takes the component `data` of the argument geodata, if provided.
locations	an $N \times 2$ matrix or data-frame with the 2-D coordinates of the N prediction locations.
cov.pars	a vector with 2 elements or an $n \times 2$ matrix with the covariance parameters σ^2 (partial sill) and ϕ (range parameter). If a vector, the elements are the values of σ^2 and ϕ, respectively. If a matrix, corresponding to a model with several structures, the values of σ^2 are in the first column and the values of ϕ are in the second.
nugget	the value of the nugget variance parameter τ^2. Defaults to zero.
micro.scale	micro-scale variance. If different from zero, the nugget variance is divided into 2 terms: *micro-scale variance* and *measurement error*. This might affect the precision of the predictions. In practice, these two variance components are usually indistinguishable but the distinction can be made here if justifiable.
cov.model	string indicating the name of the model for the correlation function. Further details in the documentation for `cov.spatial`.
kappa	additional smoothness parameter required by the following correlation functions: `"matern"`, `"powered.exponential"`, `"gneiting"` and `"gneiting.matern"`.
lambda	numeric value of the Box-Cox transformation parameter. The value $\lambda = 1$ corresponds to no transformation and $\lambda = 0$ corresponds to the log-transformation. Prediction results are back-transformed and returned is the same scale as for the original data.
m0	The default value `"ok"` indicates that ordinary kriging will be performed. Other options are `"kt"` for kriging with a trend model (universal kriging) and `"kte"` for kriging with external trend (covariates). If a numeric value is provided it is assumed to be the value of a know mean and simple kriging is then performed. If `"av"` the arithmetic mean of the data is assumed to be the know mean for simple kriging algorithm.
nwin	If `"full"` *global neighborhood* is used i.e., all data values are used in the prediction of every prediction location. An integer number defines the *moving neighborhood* algorithm. The number provided is used as the number closest neighbors to be used for the prediction at each location. Defaults to `"full"`.
n.samples.backtransform	number of samples used in the back-transformation. When transformations are used (specified by an argument `lambda`), back-transformations are usually performed by sampling from the predictive distribution and then back-transforming the sampled values. The exceptions are for $\lambda = 0$ (log-transformation) and $\lambda = 1$ (no transformation).

`trend`	only required if `m0 = "kt"` (universal kriging). Possible values are 1 or 2, corresponding to a first or second degree polynomial trend on the coordinates, respectively.
`d`	spatial dimension, 1 defines a prediction on a line, 2 on a plane (the default).
`ktedata`	only required if `m0 = "kte"`. A vector or matrix with the values of the external trend (covariates) at the data locations.
`ktelocations`	only required if `m0 = "kte"`. A vector or matrix with the values of the external trend (covariates) at the prediction locations.
`aniso.pars`	parameters for geometric anisotropy correction. If `aniso.pars = FALSE` no correction is made, otherwise a two elements vector with values for the anisotropy parameters must be provided. Anisotropy correction consists of a transformation of the data and prediction coordinates performed by the function `coords.aniso`.
`signal`	logical. If `TRUE` the signal is predicted, otherwise the variable is predicted. If no transformation is performed the expectations are the same in both cases and the difference is only for values of the kriging variance, if the value of the nugget is different from zero.
`dist.epsilon`	a numeric value. Points which are separated by a distance less than this value are considered co-located.
`messages.screen`	
	logical. Indicates whether or not status messages are printed on the screen (or other output device) while the function is running.

Value

An object of the `class kriging` which is a list with the following components:

`predict`	the predicted values.
`krige.var`	the kriging variances.
`dif`	the difference between the predicted value and the global mean. Represents the contribution to the neighboring data to the prediction at each point.
`summary`	values of the arithmetic and weighted mean of the data and standard deviations. The weighted mean corresponds to the estimated value of the global mean.
`ktrend`	the matrix with trend if `m0 = "kt"` (universal kriging).
`ktetrend`	the matrix with trend if `m0 = "kte"` (external trend kriging).
`beta`	the value of the mean which is implicitly estimated for `m0 = "ok"`, `"kte"` or `"kt"`.
`wofmean`	weight of mean. The predicted value is an weighted average between the global mean and the values at the neighboring locations. The value returned is the weight of the mean.
`locations`	the coordinates of the prediction locations.
`message`	status messages returned by the algorithm.
`call`	the function call.

Note

This is a preliminary and inefficient function implementing kriging methods. For predictions using global neighborhood the function `krige.conv` should be used instead.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`krige.conv` for a more efficient implementation of conventional kriging methods,
`krige.bayes` for Bayesian prediction.

Examples

```
if(is.R()) data(s100)
loci <- expand.grid(seq(0,1,l=31), seq(0,1,l=31))
kc <- ksline(s100, loc=loci, cov.pars=c(1, .25))
par(mfrow=c(1,2))
image.kriging(kc, loc=loci, main="kriging estimates")
image.kriging(kc, loc=loci, val=sqrt(kc$krige.var),
              main="kriging std. errors")
```

`likfit.old`	*Likelihood Estimation for Gaussian Random Fields*

Description

This function estimates the parameters of a (transformed) Gaussian random field using either *maximum likelihood* (ML) or *restricted maximum likelihood* (REML). Includes option for the estimation the Box-Cox transformation parameter.

This is a earlier version of the function `likfit` and it will be made obsolete.

Usage

```
likfit(geodata, coords=geodata$coords, data=geodata$data,
       trend = "cte", ini, fix.nugget = FALSE, nugget = 0,
       cov.model = c("exponential", "matern", "gaussian",
                     "spherical", "circular", "cubic", "wave",
                     "powered.exponential", "cauchy", "gneiting",
                     "gneiting.matern", "pure.nugget"),
       kappa = 0.5, fix.lambda = TRUE, lambda = 1, method = "ML",
       predicted = FALSE, residuals = FALSE,
       minimisation.function = c("optim","nlmP", "nlm"),
       automatic.refit = FALSE, range.limits,
       messages.screen = TRUE, ...)
```

Arguments

geodata	a list containing the elements `coords` and `data` as described next. If not provided the arguments `coords` and `data` must be provided instead.
coords	an $n \times 2$ matrix containing in each row Euclidean coordinates of the n data locations. By default it takes the element `coords` of the argument `geodata`.
data	a vector with data values. By default it takes the element `data` of the argument `geodata`.
trend	specifies the mean part of the model. The options are: `"cte"` (constant mean - the default option), `"1st"` (a first degree polynomial on the coordinates), `"2nd"` (a second degree polynomial on the coordinates), or a formula of the type `~X` where X is a matrix with the covariates (external trend).
ini	initial values of the covariance parameters. These values are used to start the numerical minimizer. If the model to be fitted has the following 3 parameters: nugget (τ^2), sill (σ^2) and range (ϕ), `ini` should be a 3 elements vector with initial values for these three parameters, in this order. If the model to be fitted does not includes the nugget parameter, `ini` is a vector with 2 components, the initial values for σ^2 and ϕ, respectively. If a matrix with several initial values on the rows is provided, a search for the best initial value is performed first, taking the one which maximizes the likelihood.
fix.nugget	logical, indicating whether or not the nugget parameter must be included in the estimation. If `fix.nugget = T` the argument `ini` must be a vector of length 2 or a matrix with 2 columns
nugget	value for the nugget parameter when `fix.nugget = TRUE`. Defaults to zero.
cov.model	correlation function model. See documentation for the function `cov.spatial`.
kappa	extra smoothness parameter required if one of the following correlation function is used: `"matern"`, `"powered.exponential"`, `"gneiting"` or `"gneiting.matern"`). For more details see documentation for the function `cov.spatial`. In this implementation this parameter is always regarded as fixed during the ML/REML parameter estimation.
fix.lambda	If `TRUE`, the default, the transformation parameter is regarded as fixed (known) during the estimation process, otherwise the ML/REML for this parameter is also computed.
lambda	the value of the Box-Cox transformation parameter. Two particular cases are $\lambda = 1$ which corresponds to no transformation and $\lambda = 0$ corresponding to the log-transformation. The value of the transformation parameter λ is regarded as a fixed if `fix.lambda = TRUE` otherwise, it is used as a initial value.
method	`"ML"` defines maximum likelihood and `"REML"` defines restricted maximum likelihood. Defaults to `"ML"`.
predicted	a matrix with the values for the components of the predicted values at the data locations as defined by the model adopted.
residuals	a matrix with values for the components of the random part of the model at the data locations.

`automatic.refit`

>   Defaults to `FALSE`. If set to `TRUE` the model is automatically changed and
>   re-fitted in the following cases:
>
>   - if the model includes the nugget and if the estimated relative nugget
>   is less than 0.01, the model without nugget is fitted.
>   - if the estimated range parameter is less than $1e - 12$ or a value pro-
>   vided in the argument `range.limits`, a model without spatial corre-
>   lation is fitted.

`minimisation.func`

>   minimization function to be used.   Options are `"optim"`, the default,
>   `"nlmP"` and `"nlm"`.

`range.limits` minimum and maximum values allowed for the parameter ϕ, the range
>   parameter. Defaults to `c(0, +Inf)`.

`messages.screen`

>   logical. Indicates whether or not status messages are printed on the screen
>   (or output device) while the function is running.

`...`   additional parameters to be passed to the minimization function. Typ-
>   ically `control` type arguments which controls the behavior of the mini-
>   mization algorithm. For further details see documentation for the mini-
>   mization functions.

Details

The random field model considered here has the following parameters:

- the mean parameter β,
- the covariance parameters: partial sill σ^2 and range parameter ϕ,
- the smoothness parameter κ,
- the nugget parameter τ^2,
- the Box-Cox transformation parameter λ,
- and the anisotropy parameters: anisotropy angle ψ_A and anisotropy ratio ψ_R,

However not all of them can be estimated using this function. For this current implemen-
tation:

1. the parameters β, σ^2, ϕ are always estimated;
2. the parameters τ^2, λ can be estimated or considered fixed;
3. the parameters κ, α, ψ are always regarded as fixed values.

Value

An object of the class `variomodel` which is a list with the following components:

`cov.model`   a string with the name of the correlation function.

`nugget`   value of the nugget parameter τ^2.   This is the estimated value if
>   `fix.nugget = FALSE` or the fixed (known) value if `fix.nugget = TRUE`.

`cov.pars`   a 2 elements vector with the estimated values of the partial sill and range
>   parameter, respectively.

`kappa`   the fixed value of the smoothness parameter required by some of the
>   correlation functions.

`beta`	estimated mean parameters. Can be a scalar or vector depending on the specification of the trend part of the model (covariates).
`beta.var`	estimated variance (or covariance matrix) of the mean parameter.
`lambda`	Box-Cox transformation parameter. A fixed (know) value if `fix.lambda` = TRUE or the estimated value if `fix.lambda` = FALSE.
`loglik`	the value of the maximized likelihood.
`npars`	number of estimated parameters.
`AIC`	value of the Akaike information criteria.
`BIC`	value of the Bayesian information criteria.
`trend.ols`	trend (mean parameters) estimated by ordinary least squares (i.e. ignoring the spatial correlation).
`info.lambda`	stores information about the Box-Cox transformation parameter. Typically this is used by other functions which process the output of `likfit.old()`.
`method`	estimation method used, "ML" (maximum likelihood) or "REML" (restricted maximum likelihood).
`s2`	estimated residual variance. Only returned if `predicted` = TRUE or `residuals` = TRUE.
`predicted`	predicted values at data locations. Only returned if `predicted` = TRUE.
`residuals`	estimated residuals at data locations. Only returned if `residuals` = TRUE.
`info`	results returned by the minimization function.
`max.dist`	maximum distance between two data locations. Typically this value is used by other functions which process results from `likfit.old()`.
`trend.matrix`	the trend (covariates) matrix.
`call`	the function call.

Note

`proflik.phi`, `proflik.ftau`, `proflik.nug` are auxiliary functions which computed the value of the likelihood for models without nugget, with a fixed nugget and including nugget, respectively. These functions are internally called by the minimization function during the numerical estimation of the model parameters.

Author(s)

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`summary.variomodel`, `plot.variogram`, `lines.variogram`, and `lines.variomodel` for graphical output. Profile likelihoods can be computed by `proflik`. `olsfit` and `wlsfit` performs variogram based estimation while `krige.bayes` performs Bayesian inference. For details about the minimization functions see the documentation for `optim` and `nlm`.

Examples

```
if(is.R()) data(s100)
ml <- likfit(s100, ini=c(.5, .5), fix.nug=T)
summary(ml)
reml <- likfit(s100, ini=c(.5, .5), fix.nug=T, met="REML")
summary(reml)
plot(variog(s100))
lines(ml)
lines(reml, lty=2)
```

---

likfit   *Likelihood Based Parameter Estimation for Gaussian Random Fields*

Description

Maximum likelihood (ML) or *restricted maximum likelihood* (REML) parameter estimation for (transformed) Gaussian random fields.

Usage

```
likfit(geodata, coords = geodata$coords, data = geodata$data,
       trend = "cte", ini.cov.pars, fix.nugget = FALSE, nugget = 0,
       fix.kappa = TRUE, kappa = 0.5, fix.lambda = TRUE, lambda = 1,
       fix.psiA = TRUE, psiA = 0, fix.psiR = TRUE, psiR = 1,
       cov.model = c("matern", "exponential", "gaussian",
                     "spherical", "circular","cubic", "wave",
                     "powered.exponential", "cauchy", "gneiting",
                     "gneiting.matern", "pure.nugget"),
       method = "ML", components = FALSE, nospatial = TRUE,
       limits = likfit.limits(), messages.screen = TRUE, ...)
```

Arguments

geodata   a list containing elements `coords` and `data` as described next. Typically an object of the class "geodata" - a **geoR** data-set. If not provided the arguments `coords` and `data` must be provided instead.

coords   an $n \times 2$ matrix, each row containing Euclidean coordinates of the n data locations. By default it takes the element `coords` of the argument `geodata`.

data   a vector with data values. By default it takes the element `data` of the argument `geodata`.

trend   specifies the mean part of the model. The options are: `"cte"` (constant mean), `"1st"` (a first degree polynomial on the coordinates), `"2nd"` (a second degree polynomial on the coordinates), or a formula of the type `~X` where `X` is a matrix with the covariates (external trend). Defaults to `"cte"`.

ini.cov.pars   initial values for the covariance parameters: σ^2 (partial sill) and ϕ (range parameter).

`fix.nugget`	logical, indicating whether the parameter τ^2 (nugget variance) should be regarded as fixed (`fix.nugget` = `TRUE`) or should be estimated (`fix.nugget` = `FALSE`). Defaults to `FALSE`.
`nugget`	value of the nugget parameter. Regarded as a fixed value if `fix.nugget` = `TRUE` otherwise as the initial value for the minimization algorithm. Defaults to zero.
`fix.kappa`	logical, indicating whether the extra parameter κ should be regarded as fixed (`fix.kappa` = `TRUE`) or should be estimated (`fix.kappa` = `FALSE`). Defaults to `TRUE`.
`kappa`	value of the extra parameter κ. Regarded as a fixed value if `fix.kappa` = `TRUE` otherwise as the initial value for the minimization algorithm. Defaults to 0.5. This parameter is valid only if the covariance function is one of: `"matern"`, `"powered.exponential"`, `"gneiting"` or `"gneiting.matern"`. For more details on covariance functions see documentation for `cov.spatial`.
`fix.lambda`	logical, indicating whether the Box-Cox transformation parameter λ should be regarded as fixed (`fix.lambda` = `TRUE`) or should be be estimated (`fix.lambda` = `FALSE`). Defaults to `TRUE`.
`lambda`	value of the Box-Cox transformation parameter λ. Regarded as a fixed value if `fix.lambda` = `TRUE` otherwise as the initial value for the minimization algorithm. Defaults to 1. Two particular cases are $\lambda = 1$ indicating no transformation and $\lambda = 0$ indicating log-transformation.
`fix.psiA`	logical, indicating whether the anisotropy angle parameter ψ_R should be regarded as fixed (`fix.psiA` = `TRUE`) or should be estimated (`fix.psiA` = `FALSE`). Defaults to `TRUE`.
`psiA`	value (in radians) for the anisotropy angle parameter ψ_A. Regarded as a fixed value if `fix.psiA` = `TRUE` otherwise as the initial value for the minimization algorithm. Defaults to 0. See `coords.aniso` for further details on anisotropy correction.
`fix.psiR`	logical, indicating whether the anisotropy ratio parameter ψ_R should be regarded as fixed (`fix.psiR` = `TRUE`) or should be estimated (`fix.psiR` = `FALSE`). Defaults to `TRUE`.
`psiR`	value, always greater than 1, for the anisotropy ratio parameter ψ_R. Regarded as a fixed value if `fix.psiR` = `TRUE` otherwise as the initial value for the minimization algorithm. Defaults to 1. See `coords.aniso` for further details on anisotropy correction.
`cov.model`	a string indication the model for the correlation function. For further details see documentation for `cov.spatial`.
`method`	options are `"ML"` for maximum likelihood and `"REML"` for restricted maximum likelihood. Defaults to `"ML"`.
`components`	an $n \times 3$ data-frame with fitted values for the three model components: trend, spatial and residuals. See the section DETAILS below for the model specification.
`nospatial`	logical. If `TRUE` parameter estimates for the model without spatial component are included in the output.
`limits`	values defining lower and upper limits for the model parameters used in the numerical minimization. The auxiliary function `likfit.limits()` is called to set the limits.

`messages.screen`
        logical indications whether status messages should be printed on the screen (or output device) while the function is running.

`...`
        additional parameters to be passed to the minimization function. Typically arguments of the type `control()` which controls the behavior of the minimization algorithm. For further details see documentation for the minimization function `optim`.

Details

This function estimate the parameters of the Gaussian random field model, specified here by:

$$Y(x) = \mu(x) + S(x) + e$$

where

- x defines a spatial location. Typically Euclidean coordinates on a plane.
- Y is the variable been observed.
- $\mu(x) = X\beta$ is the mean component of the model (trend).
- $S(x)$ is a stationary Gaussian process with variance σ^2 (partial sill) and a correlation function parametrized by ϕ (the range parameter). Possible extra parameters for the correlation function are the smoothness parameter κ and the anisotropy parameters ϕ_R and ϕ_A (anisotropy ratio and angle, respectively).
- e is the error term with variance parameter τ^2 (nugget variance).

The additional parameter λ allows the Box-Cox transformation. If used $Y(x)$ above is replaced by $g(Y(x))$ such that

$$g(Y(x)) = \frac{Y^\lambda(x) - 1}{\lambda}.$$

Two cases of particular interest are $\lambda = 1$ indicating no transformation and $\lambda = 0$ indicating log-transformation.

Parameter estimation is performed numerically using the R function `optim` to minimize the negative log-likelihood computed by `negloglik.GRF`.

Lower and upper limits for parameter values can be individually specified using the function `likfit.limits()`. For example, including the following in the function call:
`limits = likfit.limits(phi=c(0, 10), lambda=c(-2.5, 2.5))`,
will change the limits for the parameters ϕ and λ. Default values are used if the argument `limits` is not provided.

If the `fix.lambda = FALSE` and `nospatial = FALSE` the Box-Cox parameter for the model without the spatial component is obtained numerically, with log-likelihood computed by the function `boxcox.ns`.

Value

An object of the classes `"likGRF"` and `"variomodel"`.
The function `summary.likGRF` is used to print a summary of the fitted model.
The object is a list with the following components:

`cov.model`
        a string with the name of the correlation function.

`nugget`
        value of the nugget parameter τ^2. This is an estimate if `fix.nugget = FALSE` otherwise, a fixed value.

`cov.pars`	a vector with the estimates of the parameters σ^2 and ϕ, respectively.
`kappa`	value of the smoothness parameter. Valid only if the correlation function is one of: `"matern"`, `"powered.exponential"`, `"gneiting"` or `"gneiting.matern"`.
`beta`	estimate of mean parameter β. This can be a scalar or vector depending on the trend (covariates) specified in the model.
`beta.var`	estimated variance (or covariance matrix) for the mean parameter β.
`lambda`	values of the Box-Cox transformation parameter. A fixed value if `fix.lambda = TRUE` otherwise the estimate value.
`aniso.pars`	fixed values or estimates of the anisotropy parameters, according to the function call.
`method`	estimation method used, `"ML"` (maximum likelihood) or `"REML"` (restricted maximum likelihood).
`loglik`	the value of the maximized likelihood.
`npars`	number of estimated parameters.
`AIC`	value of the Akaike information criteria.
`BIC`	value of the Bayesian information criteria.
`parameters.summary`	a data-frame with all model parameters, their status (estimated or fixed) and values.
`info.minimisation`	results returned by the minimisation function.
`max.dist`	maximum distance between 2 data points. This information relevant for other functions which use outputs from `likfit`.
`trend.matrix`	the trend (covariates) matrix X.
`log.jacobian`	numerical value of the logarithm of the Jacobian of the transformation.
`nospatial`	estimates for the model without the spatial component.
`call`	the function call.

Author(s)

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`summary.likGRF` for summary of the results, `plot.variogram`, `lines.variogram` and `lines.variomodel` for graphical output, `proflik` for computing profile likelihoods, `olsfit` and `wlsfit` for other estimation methods, and `optim` for the numerical minimization function.

Examples

```
if(is.R()) data(s100)
ml <- likfit(s100, ini=c(0.5, 0.5), fix.nug = TRUE)
ml
summary(ml)
reml <- likfit(s100, ini=c(0.5, 0.5), fix.nug = TRUE, met = "REML")
summary(reml)
plot(variog(s100))
lines(ml)
lines(reml, lty = 2)
```

`lines.grf`	*Lines with True Variogram for Simulated Data*

Description

This functions adds to the graphics device a line with the theoretical (true) variogram used when generating simulations with the function `grf`.

Usage

```
lines.grf(obj, max.dist = max(dist(obj$coords)), length = 100,
          lwd = 2, ...)
```

Arguments

`obj`	an object from the class `grf` typically an output of the function `grf`.
`max.dist`	maximum distance to compute and plot the true variogram. Defaults to the maximum distance between two data locations.
`length`	number of points used to compute and draw the variogram line.
`lwd`	width of the line.
`...`	further arguments to be passed to the function `lines`.

Value

A line with the true variogram model is added to the current plot on the graphics device. No values are returned.

Author(s)

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`grf`, `plot.grf`, `lines`.

Examples

```
sim <- grf(100, cov.pars=c(1, .25)) # simulates data
plot(variog(sim, max.dist=1))        # plot empirical variogram
lines(sim, max.dist=1)               # plot true variogram
```

`lines.krige.bayes`   *Add a (Bayesian) Estimated Variogram to a Plot*

Description

Adds a estimated variogram to a plot with an empirical variogram. The estimate is a chosen summary (mean, mode or mean) of the posterior distribution returned by the function `krige.bayes`.

Usage

```
lines.krige.bayes(obj, max.dist, length = 100,
            summary.posterior = c("mode", "median", "mean"), ...)
```

Arguments

`obj`	an object of the class `krige.bayes`, typically output of the function `krige.bayes`.
`max.dist`	maximum distance for the x-axis.
`length`	number of points to compute the variogram values.
`summary.posterior`	
	specify which summary of the posterior distribution should be used as parameter estimation. Options are `"mean"`, `"median"` or `"mode"`.
`...`	arguments to be passed to the function `lines`.

Value

A line with the estimated variogram plot is added to the plot in the current graphics device. No values are returned.

Author(s)

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Peter J. Diggle ⟨p.diggle@lancaster.ac.uk⟩.

References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`krige.bayes` and `lines`.

Examples

```
#See examples in the documentation of the function krige.bayes().
```

---

lines.variogram.envelope

Adds Envelopes Lines to a Variogram Plot

Description

Variogram envelopes computed by `variog.model.env` or `variog.mc.env` are added to the current variogram plot.

Usage

```
lines.variogram.envelope(obj, lty = 3, ...)
```

Arguments

obj   an object of the class `"variogram.envelope"`, typically an output of the functions `variog.model.env` or `variog.mc.env`.

lty   line type. Defaults to 3.

...   arguments to be passed to the function `lines`.

Value

Lines defining the variogram envelope are added to the plotin the current graphics device.

Author(s)

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`variog` for variogram computation, `variog.model.env` and `variog.mc.env` for computation of variogram envelopes, and `lines` for the generic function.

Examples

```
if(is.R()) data(s100)
s100.vario <- variog(s100, max.dist = 1)
s100.ml <- likfit(s100, ini=c(.5, .5))
s100.mod.env <- variog.model.env(s100, obj.variog = s100.vario,
    model = s100.ml)
s100.mc.env <- variog.mc.env(s100, obj.variog = s100.vario)
plot(s100.vario)
lines(s100.mod.env)
lines(s100.mc.env, lwd=2)
```

`lines.variogram`	*Line with a Empirical Variogram*

Description

A sample (empirical) variogram computed using the function `variog` is added to the current plot.

Usage

```
lines.variogram(obj, max.dist = max(obj$u), type = "o",
                scaled = F, ...)
```

Arguments

`obj`	an object of the class `"variogram"`, typically an output from the function `variog`.
`max.dist`	maximum distance for the x-axis. The default is the maximum distance for which the sample variogram was computed.
`type`	type of line for the empirical variogram. The default is `"o"` (dots and lines). See documentation for `lines` for further details.
`scaled`	logical. If `TRUE` the variogram values are divided by the sample variance. This allows comparison between variograms of different variables.
`...`	other arguments to be passed to the function `lines`.

Value

A line with the empirical variogram is added to the plot in the current graphics device. No values are returned.

Author(s)

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`variog`, `lines.variogram`, `lines.variomodel`, `variog.model.env`, `variog.mc.env`, `plot.grf`, `lines`.

`lines.variomodel`   *Line with a Variogram Model*

Description

This function adds a theoretical and/or fitted variogram to the current plot. The variogram model to be added is typically an output of a variogram estimation function. Alternatively a model cab be specified by the user.

Usage

```
lines.variomodel(obj, max.dist = obj$max.dist, length = 100, ...)
```

Arguments

`obj`	an object of the class `variomodel` which is a list containing information about the model parameters.
`max.dist`	maximum distance (x-axis) to compute and draw the line representing the variogram model. The default is the distance given by `obj$max.dist`.
`length`	number of points between `0` and `max.dist` to compute the values of the variogram model.
`...`	arguments to be passed to the function `lines`.

Details

Allows theoretical and/or fitted variogram(s) be added to a plot. Together with `plot.variogram` can be used to compare sample variograms against fitted models returned by `olsfit`, `wlsfit` and/or `likfit`.

Value

A line with a variogram model is added to a plot on the current graphics device. No values are returned.

Author(s)

Paulo Justiniano Ribeiro Jr. ⟨Paulo.Ribeiro@est.ufpr.br⟩,
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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`plot.variogram`, `lines.variogram`, `olsfit`, `wlsfit`, `likfit`, `lines`.

Examples

```
sim <- grf(100, cov.pars=c(1, .3))
# generates simulated data
vario <- variog(sim)
# computes empirical variogram
plot(vario)
# plots the empirical variogram
vario.wls <- wlsfit(vario, ini=c(1, .3), fix.nugget = T)
# estimate parameters
lines(vario.wls)
# adds fitted model to the plot
```

---

matern   *Computer Values of the Matern Correlation Function*

Description

This function computes values of the Matérn correlation function for given distances and parameters.

Usage

```
matern(u, phi, kappa)
```

Arguments

u   a vector, matrix or array with values of the distances between pairs of data locations.

phi   value of the range parameter ϕ.

kappa   value of the smoothness parameter κ.

Details

The Matérn model is defined as:

$$\rho(u; \phi, \kappa) = \{2^{\kappa-1}\Gamma(\kappa)\}^{-1}(u/\phi)^{\kappa}K_{\kappa}(u/\phi)$$

where ϕ and κ are parameters and $K_{\kappa}(\cdot)$ denotes the modified Bessel function of the third kind of order κ. The family is valid for $\phi > 0$ and $\kappa > 0$.

Value

A vector matrix or array, according to the argument u, with the values of the Matérn correlation function for the given distances.

Author(s)

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`cov.spatial` for the correlation functions implemented in **geoR**, and `besselK` for computation of the Bessel functions.

Examples

```
dval <- seq(0,1,l=101)
#
# Models with fixed range and varying smoothness parameter
#
mat.5 <-  matern(dval, phi = .25, kappa = 0.5)
mat1 <-  matern(dval, phi = .25, kappa = 1)
mat2 <-  matern(dval, phi = .25, kappa = 2)
mat3 <-  matern(dval, phi = .25, kappa = 3)
plot(0:1, 0:1, type="n", xlab="distance", ylab=expression(rho(h)),
main=expression(paste("varying  ", kappa, "  and fixed  ", phi)))
lines(dval, mat.5, lty=2)
lines(dval, mat1)
lines(dval, mat2, lwd=2, lty=2)
lines(dval, mat3, lwd=2)
legend(0.6,1, c(expression(kappa == 0.5), expression(kappa == 1),
    expression(kappa == 2), expression(kappa == 3)),
    lty=c(2,1,2,1), lwd=c(1,1,2,2))
#
# Correlations with equivalent "practical range"
# and varying smoothness parameter
#
mat.5 <-  matern(dval, phi = .25, kappa = 0.5)
mat1 <-  matern(dval, phi = .188, kappa = 1)
mat2 <-  matern(dval, phi = .140, kappa = 2)
mat3 <-  matern(dval, phi = .117, kappa = 3)
plot(0:1, 0:1, type="n", xlab="distance", ylab=expression(rho(h)),
    main="models with the equivalent \"practical\" range")
lines(dval, mat.5, lty=2)
lines(dval, mat1)
lines(dval, mat2, lwd=2, lty=2)
lines(dval, mat3, lwd=2)
legend(0.5,1, c(expression(paste(kappa == 0.5, "  and  ",
    phi == 0.250)),
    expression(paste(kappa == 1, "  and  ", phi == 0.188)),
    expression(paste(kappa == 2, "  and  ", phi == 0.140)),
    expression(paste(kappa == 3, "  and  ", phi == 0.117))),
    lty=c(2,1,2,1), lwd=c(1,1,2,2))
```

---

nlmP   *Adapts nlm for Constraints in the Parameter Values*

Description

This function adapts the R function `nlm` to allow for constraints (upper and/or lower bounds) in the values of the parameters.

Usage

```
nlmP(objfunc, params, lower=rep(-Inf, length(params)),
     upper=rep(+Inf, length(params)), ...)
```

Arguments

`objfunc`	the function to be minimized.
`params`	starting values for the parameters.
`lower`	lower bounds for the variables. Defaults to $-Inf$.
`upper`	upper bounds for the variables. Defaults to $-Inf$.
`...`	further arguments to be passed to the function `nlm`.

Details

Constraints on the parameter values are internally imposed by using exponential, logarithmic, and logit transformation of the parameter values.

Value

The output is the same as for the function `nlm`.

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Adapted and included in **geoR** by
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Peter J. Diggle ⟨p.diggle@lancaster.ac.uk⟩.

References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`nlm`, `optim`.

Description

Fits a variogram model to an empirical variogram. Variogram parameters are estimated by ordinary least squares.

Usage

```
olsfit(vario, ini.cov.pars,
       cov.model = c("exponential", "matern", "gaussian",
                     "spherical", "circular", "cubic", "wave",
                     "powered.exponential", "cauchy", "gneiting",
                     "gneiting.matern", "pure.nugget"),
       fix.nugget = FALSE, nugget = 0, kappa = NULL,
       simul.number = NULL, max.dist = "all",
       minimisation.function = c("optim", "nlm", "nls"), lower = 0,
       messages.screen = TRUE)
```

Arguments

vario	an object of the class "variogram", typically an output of the function variog. The object is a list with information about the empirical variogram.
ini.cov.pars	initial values for the covariance parameters: σ^2 (partial sill) and ϕ (range parameter). See DETAILS below.
cov.model	a string with the name of the correlation function. For further details see documentation for cov.spatial. Defaults to "exponential".
fix.nugget	logical, indicating whether the parameter τ^2 (nugget variance) should be regarded as fixed (fix.nugget = TRUE) or should be estimated (fix.nugget = FALSE). Defaults to FALSE.
nugget	value for the nugget parameter. Regarded as a fixed values if fix.nugget = TRUE or as a initial value for the minimization algorithm if fix.nugget = FALSE. Defaults to zero.
kappa	fixed value of the smoothness parameter, only required by the following correlation functions: "matern", "powered.exponential", "gneiting" and "gneiting.matern".
simul.number	number of simulation. To be used when the object passed to the argument vario has empirical variograms for more than one data-set (or simulation). Indicates to which one the model will be fitted.
max.dist	maximum distance considered when fitting the variogram. Defaults to vario$max.dist.
minimisation.function	
	minimization function used to estimate the parameters. Options are "optim", "nlm", "nls". Defaults to "optim".
lower	lower limits for the parameter values. Defaults to zero.

`messages.screen`

> logical. Indicates whether or not status messages are printed on the screen (or other output device) while the function is running.

`...`

> further parameters to be passed to the minimization function. Typically arguments of the type `control()` which controls the behavior of the minimization algorithm. See documentation for the selected minimization function for further details.

Details

Initial values

The algorithms for minimization functions require initial values of the parameters.

A unique initial value is used if a vector is provided in the argument `ini.cov.pars`. The elements are initial values for σ^2 and ϕ, respectively. This vector is concatenated with the value of the argument `nugget` if `fix.nugget = FALSE`.

Specification of multiple initial values is also possible. If this is the case, the function searches for the one which minimizes the loss function and uses this as the initial value for the minimization algorithm. Multiple initial values are specified by providing a matrix in the argument `ini.cov.pars` and/or, if `fix.nugget = FALSE`, providing a vector with length greater than one for the argument `nugget`. If `ini.cov.pars` is a matrix, the first column has values of σ^2 and the second has values of ϕ.

Value

An object of the `class "variomodel"` which is list with the following components:

`nugget`

> value of the nugget parameter. An estimated value if `fix.nugget = FALSE` or a fixed value if `fix.nugget = TRUE`.

`cov.pars`

> a two elements vector with estimated values of the covariance parameters σ^2 and ϕ, respectively.

`cov.model`

> a string with the name of the correlation function.

`kappa`

> fixed value of the smoothness parameter.

`value`

> minimized value of the loss function.

`max.dist`

> maximum distance considered in the variogram fitting.

`minimisation.function`

> minimization function used.

`message`

> status messages returned by the function.

`method`

> a string `"OLS"` indicating the estimation method which was used.

`call`

> the function call.

Author(s)

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Peter J. Diggle ⟨p.diggle@lancaster.ac.uk⟩.

References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

cov.spatial for a detailed description of the available correlation (variogram) functions, wlsfit for weighted least squares variogram fit, likfit for maximum and restricted maximum likelihood estimation, lines.variomodel for graphical output of the fitted model. For details on the minimization functions see optim, nlm and nls.

Examples

```
if(is.R()) data(s100)
vario100 <- variog(s100, max.dist=1)
ini.vals <- expand.grid(seq(0,1,l=5), seq(0,1,l=5))
ols <- olsfit(vario100, ini=ini.vals, fix.nug=TRUE)
summary(ols)
plot(vario100)
lines(ols)
```

---

parana   *Rainfall Data from Parana State, Brasil*

Description

This data-set was used by Diggle and Ribeiro (2001) to illustrate the methods discussed in the paper. The data reported analysis was carried out using the package **geoR**.

The data refers to average rainfall over different years for the period May-June (dry-season). It was collected at 143 recording stations throughout Paraná State, Brasil.

Usage

data(parana)

Format

Three objects are provided:

maijun a list with coordinates of the recording stations and the May-June average data.

borders a matrix with the coordinates defining the borders of Paraná state.

loci.paper a matrix with the coordinates of the four prediction locations discussed in the paper.

Source

The data were collected at several recording stations at Paraná State, Brasil, belonging to the following companies: COPEL, IAPAR, DNAEE, SUREHMA and INEMET.

The data base was organized by Laura Regina Bernardes Kiihl (IAPAR, Instituto Agronômico do Paraná, Londrina, Brasil) and the fraction of the data included in this data-set was provided by Jacinta Loudovico Zamboti (Universidade Estadual de Londrina, Brasil). The coordinates of the borders of Paraná State were provided by João Henrique Caviglione (IAPAR).

References

Diggle, P.J. and Ribeiro Jr, P.J. (2001). Bayesian inference in Gaussian model-based geo-statistics. *Geographical and Environmental Modeling* (to appear)

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

---

plot.geodata	*Exploratory Geostatistical Plots*

Description

This function produces a 2 × 2 graphics display with the following plots: the first indicates spatial locations, the second is a 3-D plot with spatial locations and associated data values (or a histogram of the data), and the last two shows data against the X and Y coordinates.

Usage

```
plot.geodata(geodata, coords=geodata$coords, data = geodata$data,
      trend="cte", lambda = 1, col.data = 1, weights.divide = FALSE,
      window.new = FALSE, ...)
```

Arguments

geodata   a list containing elements `coords` and `data` described next. Typically an object of the class `"geodata"` - a **geoR** data-set. If not provided the arguments `coords` and `data` must be provided instead.

coords   an $n \times 2$ matrix containing in each row Euclidean coordinates of the n data locations. By default it takes the element `coords` of the argument `geodata`.

data   a vector with data values. By default it takes the element `data` of the argument `geodata`.

trend   specifies the mean part of the model. The options are: `"cte"` (constant mean - default option), `"1st"` (a first degree polynomial on the coordinates), `"2nd"` (a second degree polynomial on the coordinates), or a formula of the type `~X` where X is a matrix with the covariates (external trend). If provided the trend is "removed" using the function `lm` and the residuals are plotted.

lambda   value of the Box-Cox transformation parameter. Two particular cases are $\lambda = 1$ which corresponds to no transformation and $\lambda = 0$ corresponding to the log-transformation.

col.data   indicates the number of the column of the data to be plotted. Only valid if more than one data-set is available i.e., if the argument `data` is a matrix.

weights.divide
                if a vector of weights with the same length as the data is provided each data is divided by the corresponding element in this vector. Defaults to `NULL`.

window.new   logical. If `TRUE` a new graphic device is openned, otherwise the current one is used. Defaults to `FALSE`.

...   further arguments to be passed to the function `scatterplot3d`.

Details

By default, this function requires the package *scatterplot3d* in order to produce a 3-D plot with data locations and coordinates. If this package is not available an histogram of the data replaces the 3-D plot.

Value

A plot is produced on the graphics device. No values are returned.

Author(s)

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`points.geodata`, `scatterplot3d`.

Examples

```
if(is.R()) data(s100)
plot(s100)
```

`plot.grf`	*Plots Variograms for Simulated Data*

Description

This function plots variograms for simulated geostatistical data generated by the function `grf`.

Usage

```
plot.grf(obj, model.line = TRUE, plot.grid = FALSE,
         ylim = "default", ...)
```

Arguments

`obj`	an object of the class `grf`, typically an output of the function `grf`.
`model.line`	logical. If `TRUE` the true variogram model is added to the plot with the sample variogram(s).
`plot.grid`	logical. If `TRUE` a plot with data locations is also shown.
`ylim`	limits for the y-axis. The default is the maximum value of the variogram among all of the simulations.
`...`	further arguments to be passed to the functions `variog` and `plot`.

Value

A plot with the empirical variogram(s) is produced on the output device. No values are returned.

Author(s)

Paulo Justiniano Ribeiro Jr. ⟨Paulo.Ribeiro@est.ufpr.br⟩,
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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

grf for simulation of Gaussian random fields, plot.variogram for plotting empirical variogram, variog for computation of empirical variograms and plot for the generic plotting function.

Examples

```
par(mfrow=c(2,1))
sim1 <- grf(100, cov.pars=c(10, .25))
# generates simulated data
plot(sim1, grid=T)
# plots the locations and the sample true variogram model
#
par(mfrow=c(1,1))
sim2 <- grf(100, cov.pars=c(10, .25), nsim=10)
# generates 10 simulated data
plot(sim1)
# plots sample variograms for all simulations with the true model
```

---

plot.proflik	*Plots Profile Likelihoods*

Description

This function produces plots with the profile likelihoods computed by the function proflik.

Usage

```
plot.proflik(obj.proflik, pages = c("user", "one", "two"),
     uni.only = FALSE, bi.only = F,
     type.bi = c("contour", "persp"), conf.int = c(0.9, 0.95),
     yaxis.lims = c("conf.int", "as.computed"),
     by.col = TRUE, log.scale = FALSE,
     par.mar.persp = c(0, 0, 0, 0), ...)
```

Arguments

`obj.proflik`	an object of the class `proflik`, typically an output of the function `proflik`.
`pages`	specify how the plots will be arranged in the graphics device. The default option, `"user"`, uses the current graphical parameters. The option `"one"` places all the profiles in the same page and the option `"two"` places the univariate profiles in one page and the bivariate profiles in a second page.
`uni.only`	only 1-D profiles are plotted even if the object contains results about the 2-D profiles.
`bi.only`	only 2-D profile are plotted even if the object contains results about the 1-D profiles.
`type.bi`	Type of plot for the 2-D profiles. Options are `"contour"` for contour plot (the default) and `"persp"` for perspective plot.
`conf.int`	a vector with numbers in the interval $[0, 1]$ specifying levels of the (approximated) confidence intervals. Defaults corresponds to the levels 90% and 95%.
`yaxis.lims`	defines the lower limits for the y-axis in the 1-D plots. If `"conf.int"` the limit is determined by the level of the confidence interval (the default) otherwise will be determined by the smallest computed value.
`by.col`	logical, If `TRUE` the plots are arranged by columns in a multiple graphics device.
`log.scale`	plots the x-axis in the logarithmic scale. Defaults to `FALSE`.
`...`	additional arguments to be passed to the functions `plot`, `contour` and/or `persp`.

Value

Produces plots with the profile likelihoods on the current graphics device. No values are returned.

Author(s)

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`proflik` for computation of the profile likelihoods. For the genneric plotting functions see `plot`, `contour` and `persp`.

Examples

```
# see examples in the documentation for the function proflik()
```

plot.variogram	*Plot Empirical Variogram*

Description

Plots sample (empirical) variogram computed using the function `variog`.

Usage

```
plot.variogram(obj, max.dist = max(obj$u), ylim = "default",
               type = "b", scaled = FALSE, var.lines = FALSE,
               envelope.obj = NULL, bin.cloud = FALSE, ...)
```

Arguments

`obj`	an object of the class `"variogram"`, typically an output of the function `variog`.
`max.dist`	maximum distance for the x-axis. The default is the maximum distance for which the sample variogram was computed.
`ylim`	limits for the variogram values in the y-axis. The default is from 0 to the maximum value in `obj$v`.
`type`	type of line for the empirical variogram. The default is `"b"` (dots and lines). For further details see documentation for `lines`.
`scaled`	If `TRUE` the variogram values are divided by the sample variance. This allows comparison between variograms from different variables.
`var.lines`	If `TRUE` a horizontal line is drawn at the value of the variance of the data (if `scaled = F`) or at 1 (if `scaled = T`).
`envelope.obj`	adds a variogram envelope computed by the function `variog.model.env` or `variog.mc.env`.
`bin.cloud`	logical. If `TRUE` and the sample variogram was computed with the option `keep.cloud = TRUE`, box-plots of values at each bin are plotted instead of the empirical variograms.
`...`	other arguments to be passed to the function `plot`.

Details

This function allows visualization of sample variogram and together with `lines.variogram` can be used to compare sample variograms for different variables. Furthermore, together with `lines.variomodel` can be used to compare theoretical and/or fitted variogram models against the empirical variogram.

Value

Produces a plot with the sample variogram on the current graphics device. No values are returned.

Author(s)

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Peter J. Diggle ⟨p.diggle@lancaster.ac.uk⟩

References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`variog` for variogram calculations, `lines.variogram` and `lines.variomodel` for adding lines to the current plot, `variog.model.env` and `variog.mc.env` for variogram envelops computation, and `plot` for generic plot function.

Examples

```
sim <- grf(100, cov.pars=c(1, .2))# generates simulated data
vario <- variog(sim, max.dist=1)  # computes sample variogram
par(mfrow=c(1,2))
plot(vario)                       # the sample variogram
plot(vario, scaled=T)             # the scaled sample variogram
```

---

points.geodata	*Plots Spatial Locations and Data Values*

Description

This function produces a plot with points indicating the data locations. Arguments can control the points sizes, patterns and colors. These can be set to be proportional to data values, ranks or quantiles. Alternatively, points can be added to the current plot.

Usage

```
points.geodata(geodata, coords=geodata$coords, data=geodata$data,
              data.col = 1,
              pt.sizes=c("data.proportional","rank.proportional",
                  "quintiles", "quartiles", "deciles", "equal"),
              cex.min, cex.max, pch.seq, col.seq,
              add.to.plot = FALSE,
              round.quantiles = FALSE, graph.pars = FALSE, ...)
```

Arguments

geodata	a list containing elements `coords` and `data` described next. Typically an object of the class `"geodata"` - a **geoR** data-set. If not provided the arguments `coords` and `data` must be provided instead.
coords	an $n \times 2$ matrix containing coordinates of the n data locations in each row. Defaults to `geodata$coords`.
data	a vector or matrix with data values. If a matrix is provided each column is regarded as one variable or realization. Defaults to `geodata$data`.
data.col	the number of the data column. Only used if `data` is a matrix with columns corresponding to different variables or simulations.
pt.sizes	defines the point sizes. See `DETAILS` below for the available options. Defaults to `pt.sizes = "data.proportional"`.

`cex.min`	minimum value for the graphical parameter `cex`. This value defines the size of the point corresponding the minimum of the data. Defaults to 0.5.
`cex.max`	maximum value for the graphical parameter `cex`. This value defines the size of the point corresponding the maximum of the data. If `pt.sizes` = `"equal"` it is used to set the value for the graphical parameter `cex`. Defaults to 1.5.
`pch.seq`	number(s) defining the graphical parameter `pch`.
`col.seq`	number(s) defining the colors in the graphical parameter `col`.
`add.to.plot`	logical. If `TRUE` the points are added to the current plot otherwise a new plot is created. Defaults to `FALSE`.
`round.quantiles`	
	logical. Defines whether or not the values of the quantiles should be rounded. Defaults to `FALSE`.
`graph.pars`	logical. If `TRUE` the graphics parameters used to produce the plots are returned. Defaults to `FALSE`.
`...`	further arguments to be passed to the function `plot`, if `add.to.plot` = `FALSE`; or to the function `points`, if `add.to.plot` = `TRUE`.

Details

The points can have different sizes according to the argument `pt.sizes`. The options are:

"data.proportional" sizes proportional to the data values.

"rank.proportional" sizes proportional to the rank of the data.

"quintiles" five different sizes according to the quintiles of the data.

"quartiles" four different sizes according to the quartiles of the data.

"deciles" ten different sizes according to the deciles of the data.

"equal" all points with the same size.

For cases where points have different sizes the arguments `cex.min` and `cex.max` set the minimum and the maximum point sizes. Additionally, `pch.seq` can set different patterns for the points and `col.seq` can be used to define colors. For example, different colors can be used for quartiles, quintiles and deciles while a sequence of gray tones (or a color sequence) can be used for point sizes proportional to the data or their ranks. For more details see the section EXAMPLES.

Value

A plot is created or points are added to the current graphics device.
By default no value is returned. However, if `graph.pars` = `TRUE` a list with graphical parameters used to produce the plot is returned. According to the input options, the list has some or all of the following components:

`quantiles`	the values of the quantiles used to divide the data.
`cex`	the values of the graphics expansion parameter `cex`.
`col`	the values of the graphics color parameter `col`.
`pch`	the values of the graphics pattern parameter `pch`.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`plot.geodata` for another display of the data and `points` and `plot` for information on the
generic R functions. The documentation of `par` provides details on graphical parameters.
For color schemes in R see `gray` and `rainbow`.

Examples

```
if(is.R()) data(s100)
points.geodata(s100, xlab="Coord X", ylab="Coord Y")
points.geodata(s100, xlab="Coord X", ylab="Coord Y",
               pt.size="rank.prop")
points.geodata(s100, xlab="Coord X", ylab="Coord Y", cex.max=1.7,
               col=gray(seq(1, 0.1, l=100)), pt.siz="equal")
               # the function gray() works only for R
points.geodata(s100, pt.sizes="quintile", xlab="Coord X",
               ylab="Coord Y")
```

---

polygrid	*Coordinates of Points Inside a Polygon*

Description

This function builds a rectangular grid and extracts points which are inside of an internal
polygonal region.

Usage

```
polygrid(xgrid, ygrid, poly, vec.inout = FALSE)
```

Arguments

`xgrid`	grid values in the x-direction.
`ygrid`	grid values in the y-direction.
`poly`	a matrix with the polygon coordinates.
`vec.inout`	logical. If `TRUE` a logical vector is included in the output indicating whether each point of the grid is inside the polygon. Defaults to `FALSE`.

Details

This function requires the package `splancs`.

The function works as follows: First it creates a grid using the R function `expand.grid` and then it uses the function `inout` from the package `splancs` to extract the points of the grid which are inside the polygon.

Within the package **geoR** this function is typically used to select points in a non-rectangular region to perform spatial prediction using `krige.bayes`, `krige.conv` or `ksline`. It is also useful to produce image or perspective plots of the prediction results.

Value

A list with components:

`xypoly`	an $n \times 2$ matrix with the coordinates of the points inside the polygon.
`vec.inout`	logical, a vector indicating whether each point of the rectangular grid is inside the polygon. Only returned if `vec.inout = TRUE`.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`expand.grid`, `inout`.

Examples

```
poly <- matrix(c(.2, .8, .7, .1, .2, .1, .2, .7, .7, .1), ncol=2)
plot(0:1, 0:1, type="n")
lines(poly)
poly.in <- polygrid(seq(0,1,l=11), seq(0,1,l=11), poly, vec=T)
points(poly.in$xy)
```

`proflik`	*Computes Profile Likelihoods*

Description

Computes profile likelihoods for model parameters previously estimated by using the function `likfit`.

Usage

```
proflik(obj.likfit, geodata, coords = geodata$coords,
        data = geodata$data, sill.values, range.values,
        nugget.values, nugget.rel.values, lambda.values,
        sillrange.values = TRUE, sillnugget.values = TRUE,
        rangenugget.values = TRUE, sillnugget.rel.values = FALSE,
        rangenugget.rel.values = FALSE, silllambda.values = FALSE,
        rangelambda.values = TRUE,  nuggetlambda.values = FALSE,
        nugget.rellambda.values = FALSE,
        uni.only = TRUE, bi.only = FALSE,
        minimisation.function = c("optim", "nlmP"), ...)
```

Arguments

`obj.likfit`	an object of the class `likfit`, typically an output of the function `likfit`.
`geodata`	a list containing elements `coords` and `data` described next. Typically an object of the class `"geodata"` - a **geoR** data-set. If not provided the arguments `coords` and `data` must be provided instead.
`coords`	an $n \times 2$ matrix containing in each row Euclidean coordinates of the n data locations. By default it takes the element `coords` of the argument `geodata`.
`data`	a vector with data values. By default it takes the element `data` of the argument `geodata`.
`sill.values`	set of values of the partial sill parameter σ^2 for which the profile likelihood will be computed.
`range.values`	set of values of the range parameter ϕ for which the profile likelihood will be computed.
`nugget.values`	set of values of the nugget parameter τ^2 for which the profile likelihood will be computed. Only used if the model was fitted using the function `likfit` with the option `fix.nugget = FALSE`.
`nugget.rel.values`	
	set of values of the relative nugget parameter τ_R^2 for which the profile likelihood will be computed. Only used if the model was fitted using the function `likfit` with the option `fix.nugget = FALSE`.
`lambda.values`	set of values of the Box-Cox transformation parameter λ for which the profile likelihood will be computed. Only to be used if the model was fitted using the function `likfit` with the option `fix.lambda = FALSE`.
`sillrange.values`	
	logical indicating whether or not the 2-D profile likelihood should be computed. Only valid if `uni.only = FALSE`.
`sillnugget.values`	
	as above.
`rangenugget.values`	
	as above.
`sillnugget.rel.values`	
	as above.
`rangenugget.rel.values`	
	as above.
`silllambda.values`	
	as above.

```
rangelambda.values
```
         as above.
```
nuggetlambda.values
```
         as above.
```
nugget.rellambda.values
```
         as above.

`uni.only`   as above.

`bi.only`   as above.

```
minimisation.function
```
         minimization function to be used. Defaults to `optim`.

`...`   additional parameters to be passed to the minimization function.

Details

The functions `proflik.*` are auxiliary functions used to compute the profile likelihoods. These functions are internally called by the minimization functions when estimating the model parameters.

Value

An object of the class `"proflik"` which is a list. Each element contains values of a parameter (or a pair of parameters for 2-D profiles) and the corresponding value of the profile likelihood. The components of the output will vary according to the input options.

Note

1. Profile likelihoods for Gaussian Random Fields are usually uni-modal. Unusual or jagged shapes can be due to the lack of the convergence in the numerical minimization for particular values of the parameter(s). If this is the case it might be necessary to pass `control` arguments to the minimization functions. The argument ... can be used for this. See documentation of the functions `optim` and/or `nlm` for further details. It's also advisable to try the different options for the `minimisation.function` argument.

2. 2-D profiles can be computed by setting the argument `uni.only = FALSE`. However, be sure first that the 2-D profiles are really wanted. Their computation can be time demanding due to the fact that computation is performed on a grid determined by the cross-product of the values defining the 1-D profiles.

3. There is no "default strategy" to find reasonable values for the x-axis. They must be found in a "try-and-error" exercise. It's recommended to use short sequences in the initial attempts. This is illustrated in the `EXAMPLE` section below.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`plot.proflik` for graphical output, `likfit` for the parameter estimation, `optim` and `nlm` for further details about the minimization functions.

Examples

```
if(is.R()) data(s100)
ml <- likfit(s100, ini=c(.5, .5), fix.nug=T)
# a first atempt to find reasonable values for the x-axis:
prof <- proflik(ml, s100, sill.values=seq(0.5, 1.5, l=4),
                range.val=seq(0.1, .5, l=4))
par(mfrow=c(1,2))
plot(prof)
# a nicer setting and now including 2-D profiles:

prof <- proflik(ml, s100, sill.values=seq(0.45, 2, l=16),
                range.val=seq(0.1, .55, l=16), uni.only=F)
par(mfrow=c(2,2))
plot(prof, nlevels=16)

par(mfrow=c(1,1))
```

---

read.geodata   *Reads and Converts Data to geoR Format*

Description

Reads data from a *ASCII* file and converts it to an object of the class geodata, the standard data format for the **geoR** package.

Usage

```
read.geodata(file, header = FALSE, coords.col = 1:2, data.col = 3,
             data.names = NULL, covar.col = NULL,
             covar.names = "header", ...)
```

Arguments

file	a string with the name of the *ASCII* file.
header	logical. Indicates whether the variables names should be read from the first line of the input file.
coords.col	a vector with the numbers of the columns containing the coordinates.
data.col	a scalar or vector with the number of the column(s) containing the data.
data.names	a string or vector of strings with names for the data columns. Only valid if there is more than one column of data. By default the names in the original object are used.
covar.col	optional. A scalar or vector with the number of the column(s) with the values of the covariate(s).
covar.names	a string or vector of strings with the name(s) of the covariates. By default the names in the original object are used.
...	further arguments to be passed to the function read.table.

Details

The function `read.table` is used to read the data from the *ASCII* file and then `as.geodata` is used to convert to an object of the `class geodata`.

Value

An object of the `class geodata`. See documentation for the function `as.geodata` for further details.

Author(s)

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`as.geodata` to convert existing R objects, `read.table`, the basic R function used to read *ASCII* files, and `list` for detailed information about lists.

`s100 and s121`	*Simulated Data-Sets which Illustrate the Usage of the Package geoR*

Description

These two simulated data sets are the ones used in the Technical Report which describes the package **geoR** (see reference below). These data-sets are used in several examples throughout the package documentation.

Usage

```
data(s100)
data(s121)
```

Format

Two objects of the `class geodata`. Both are lists with the following components:

`coords` the coordinates of data locations.

`data` the simulated data.

`cov.model` the correlation model.

`nugget` the values of the nugget parameter.

`cov.pars` the covariance parameters.

`kappa` the value of the parameter *kappa*.

`lambda` the value of the parameter *lambda*.

References

Ribeiro Jr, P.J. and Diggle, P.J. (1999). geoS: A geostatistical library for S-PLUS. Technical report ST-99-09, Dept of Maths and Stats, Lancaster University.

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

`summary.likGRF`	*Summarizes Parameter Estimation Results for Gaussian Random Fields*

Description

Summarizes results returned by the function `likfit`. Functions are *methods* for classes `likGRF` and `summary.likGRF`.

Usage

```
summary(obj, ...)
print(summary.likGRF.obj, ...)
print(obj, ...)
```

Arguments

`obj`	an object of `class` *likGRF*, typically a result of a call to `likfit`.
`...`	extra arguments for `print`. A commonly used argument is `digits` which specifies the number of digits for the numerical output. The default is given by `options()$digits`.

Details

The model specification with values of fixed and estimated parameters is printed by `summary.likGRF`. A simplified summary of the parameter estimation is printed by `print.summary.likGRF`.

Value

`print.likGRF` prints the parameter estimates and the value of the maximized likelihood.
`summary.likGRF` returns a list with main results of a call to `likfit`.
`print.summary.likGRF` prints these results on the screen (or other output device) in a "nice" way.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

likfit, print, summary.

Examples

```
# See examples for the function likfit()
```

---

summary.variomodel   *Summarize Results of Variogram Estimation*

Description

This function prints a summary of the parameter estimation results given by olsfit or wlsfit.

Usage

```
summary.variomodel(obj)
```

Arguments

obj   an object of the class "variomodel" typically an output of olsfit or
                wlsfit.

Value

Prints a summary of the estimation results on the screen or other output device.

Author(s)

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

The functions olsfit and wlsfit for variogram based estimation. For likelihood based
parameter estimation see likfit.

Examples

```
if(is.R()) data(s100)
s100.vario <- variog(s100, max.dist=1)
wls <- wlsfit(s100.vario, ini=c(.5, .5), fix.nugget = TRUE)
summary(wls)
```

---

trend.spatial   *Prepare Trend Matrix*

Description

Builds the trend matrix according to the specification of the mean part of the model.

Usage

```
trend.spatial(trend, coords = NULL)
```

Arguments

trend   specifies the mean part of the model. The options are: `"cte"` (constant
                mean - default option), `"1st"` (a first degree polynomial on the coor-
                dinates), `"2nd"` (a second degree polynomial on the coordinates), or a
                formula of the type ˜X where X is a matrix with the covariates (external
                trend).

coords   an $n \times 2$ matrix containing in each row Euclidean coordinates. Needs to
                be provided only if `trend = "1st"` or `trend = "2nd"`.

Value

An $n \times p$ trend matrix where n is the number of spatial locations and p is the number of
mean parameters in the model.

Note

This is an auxiliary function called by other **geoR** functions.

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/˜ribeiro/geoR.html.

---

varcov.spatial   *Computes Covariance Matrix and Related Results*

Description

This function builds the covariance matrix for a set of spatial locations, given the covariance
parameters. According to the input options other results related to the covariance matrix
(such as decompositions, determinants, inverse. etc) can also be returned.

Usage

```
varcov.spatial(coords = NULL, dists.lowertri = NULL,
               cov.model = c("exponential", "matern", "gaussian",
                     "spherical", "circular", "cubic", "wave",
                     "powered.exponential", "cauchy", "gneiting",
                     "gneiting.matern", "pure.nugget"),
               kappa = NULL, nugget = 0,
               cov.pars = stop("no cov.pars argument"),
               inv = FALSE, det = FALSE,
               func.inv = c("cholesky", "eigen", "svd", "solve"),
               scaled = FALSE,  only.decomposition = FALSE,
               sqrt.inv = FALSE, try.another.decomposition = TRUE,
               only.inv.lower.diag = FALSE)
```

Arguments

coords	an $n \times 2$ matrix with the coordinates of the data locations. If not provided the argument `dists.lowertri` should be provided instead.
dists.lowertri	
	a vector with the lower triangle of the matrix of distances between pairs of data points. If not provided the argument `coords` should be provided instead.
cov.model	a string indicating the type of the correlation function. More details in the documentation for `cov.spatial`.
kappa	values of the additional smoothness parameter, only required by the following correlation functions: `"matern"`, `"powered.exponential"`, `"gneiting"` and `"gneiting.matern"`.
nugget	the value of the nugget parameter τ^2.
cov.pars	a vector with 2 elements or an $ns \times 2$ matrix with the covariance parameters. The first element (if a vector) or first column (if a matrix) corresponds to the variance parameter σ^2. second element or column corresponds to the correlation function parameter ϕ. If a matrix is provided each row corresponds to the parameters of one *spatial structure*. Models with several structures are also called *nested models* in the geostatistical literature.
inv	if `TRUE` the inverse of covariance matrix is returned. Defaults to `FALSE`.
det	if `TRUE` the logarithmic of the square root of the determinant of the covariance matrix is returned. Defaults to `FALSE`.
func.inv	algorithm used for the decomposition and inversion of the covariance matrix. Options are `"chol"` for Cholesky decomposition, `"svd"` for singular value decomposition and `"eigen"` for eigenvalues/eigenvectors decomposition. Defaults to `"chol"`.
scaled	logical indicating whether the covariance matrix should be scaled. If `TRUE` the partial sill parameter σ^2 is set to 1. Defaults to `FALSE`.
only.decomposition	
	logical. If `TRUE` only the square root of the covariance matrix is returned. Defaults to `FALSE`.
sqrt.inv	if `TRUE` the square root of the inverse of covariance matrix is returned. Defaults to `FALSE`.

`try.another.decomposition`

> logical. If `TRUE` and the argument `func.inv` is one of `"cholesky"`, `"svd"` or `"solve"`, the matrix decomposition or inversion is tested and, if it fails, the argument `func.inv` is re-set to `"eigen"`.

`only.inv.lower.diag`

> logical. If `TRUE` only the lower triangle and the diagonal of the inverse of the covariance matrix are returned. Defaults to `FALSE`.

Details

The elements of the covariance matrix are computed by the function `cov.spatial`. Typically this is an auxiliary function called by other functions in the **geoR** package.

Value

The result is always list. The components will vary according to the input options. The possible components are:

`varcov`   the covariance matrix.

`sqrt.varcov`   a square root of the covariance matrix.

`lower.inverse`   the lower triangle of the inverse of covariance matrix.

`diag.inverse`   the diagonal of the inverse of covariance matrix.

`inverse`   the inverse of covariance matrix.

`sqrt.inverse`   a square root of the inverse of covariance matrix.

`log.det.to.half`

> the logarithmic of the square root of the determinant of the covariance matrix.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`cov.spatial` for more information on the correlation functions; `chol`, `solve`, `svd` and `eigen` for matrix inversion and/or decomposition.

---

variog.mc.env   *Envelops for Empirical Variograms Based on Permutation*

Description

Computes envelops for empirical variograms by permutation of the data values on the spatial locations.

Usage

```
variog.mc.env(geodata, coords = geodata$coords, data = geodata$data,
              obj.variog, nsim = 99, save.sim = FALSE,
              messages.screen = TRUE)
```

Arguments

geodata	a list containing elements `coords` and `data` as described next. Typically an object of the class `"geodata"` - a **geoR** data-set. If not provided the arguments `coords` and `data` must be provided instead.
coords	an $n \times 2$ matrix, each row containing Euclidean coordinates of the n data locations. By default it takes the element `coords` of the argument `geodata`.
data	a vector with the data values. By default it takes the element `data` of the argument `geodata`.
obj.variog	an object of the class `"variogram"`, typically an output of the function `variog`.
nsim	number of simulations used to compute the envelope. Defaults to 99.
save.sim	logical. Indicates whether or not the simulated data are included in the output. Defaults to `FALSE`.
messages.screen	
	logical. If `TRUE`, the default, status messages are printed while the function is running.

Details

The envelops are obtained by permutation. For each simulations data values are randomly allocated to the spatial locations. The empirical variogram is computed for each simulation using the same lags as for the variogram originally computed for the data. The envelops are computed by taking, at each lag, the maximum and minimum values of the variograms for the simulated data.

Value

An object of the `class "variogram.envelope"` which is a list with the following components:

u	a vector with distances.
v.lower	a vector with the minimum variogram values at each distance in u.
v.upper	a vector with the maximum variogram values at each distance in u.
simulations	a matrix with simulated data. Only returned if `save.sim = TRUE`.

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References

Further information about **geoR** can be found at:
`http://www.maths.lancs.ac.uk/~ribeiro/geoR.html`.

See Also

`variog.model.env` for envelops computed by from a model specification, `variog` for variogram calculations, `plot.variogram` and `variog.mc.env` for graphical output.

Examples

```
if(is.R()) data(s100)
s100.vario <- variog(s100, max.dist=1)
s100.env <- variog.mc.env(s100, obj.var = s100.vario)
plot(s100.vario, envelope = s100.env)
```

`variog.model.env`	*Envelops for Empirical Variograms Based on Model Parameters*

Description

Computes envelops for empirical variograms by simulating data for given model parameters.

Usage

```
variog.model.env(geodata, coords = geodata$coords, obj.variog,
                 model.pars, nsim = 99, save.sim = FALSE,
                 messages.screen = TRUE)
```

Arguments

geodata   a list containing element `coords` as described next. Typically an object of the class `"geodata"` - a **geoR** data-set. If not provided the arguments coords must be provided instead.

coords   an $n \times 2$ matrix, each row containing Euclidean coordinates of the n data locations. By default it takes the element `coords` of the argument `geodata`.

obj.variog   an object of the class `"variogram"`, typically an output of the function `variog`.

model.pars   a list with model specification and parameter values. The input is typically an object of the class `variomodel` which is an output of `likfit`, `wlsfit` or `olsfit`. This required components of list are:

- `beta`, the mean parameter. Defaults to zero.
- `cov.model`, the covariance model. Defaults to "exponential".
- `cov.pars`, the covariance parameters σ^2 and ϕ.

- `kappa`, the extra covariance parameters for some of the covariance models. Defaults to 0.5.
- `nugget`, the error component variance. Defaults to zero.
- `estimator.type`, the type of variogram estimator. Options for `"classical"` and `"robust"`. Defaults to `obj.variog$estimator`.

`nsim`   number of simulations used to compute the envelopes. Defaults to 99.

`save.sim`   logical. Indicates whether or not the simulated data are included in the output. Defaults to `FALSE`.

`messages.screen`
                   logical. If `TRUE`, the default, status messages are printed while the function is running.

Details

The envelops are computed assuming a (transformed) Gaussian random field model. Simulated values are generated at the data locations, given the model parameters. The empirical variogram is computed for each simulation using the same lags as for the original variogram of the data. The envelopes are computed by taking, at each lag, the maximum and minimum values of the variograms for the simulated data.

Value

An object of the `class "variogram.envelope"` which is a list with the components:

`u`   a vector with distances.

`v.lower`   a vector with the minimum variogram values at each distance in u.

`v.upper`   a vector with the maximum variogram values at each distance in u.

`simulations`   a matrix with the simulated data. Only returned if `save.sim = TRUE`.

Author(s)

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`variog.mc.env` for envelops computed by using data permutation, `variog` for variogram calculations, `plot.variogram` and `variog.mc.env` for graphical output. The functions `likfit`, `wlsfit` and `olsfit` are used to estimate the model parameters.

Examples

```
if(is.R()) data(s100)
s100.ml <- likfit(s100, ini = c(0.5, 0.5), fix.nugget = TRUE)
s100.vario <- variog(s100, max.dist = 1)
s100.env <- variog.model.env(s100, obj.v = s100.vario,
    model.pars = s100.ml)
plot(s100.vario, env = s100.env)
```

`variog`   *Compute Empirical Variograms*

Description

Computes sample (empirical) variograms with options for the *classical* or *robust* estimator. Output can be returned as a `binned variogram`, a `variogram cloud` or a `smoothed variogram`. Data transformation (Box-Cox) is allowed. Trends fitted by ordinary least squares can be "removed" for which case variogram for the residuals are computed.

Usage

```
variog(geodata, coords=geodata$coords, data=geodata$data,
       uvec = "default", trend = "cte", lambda = 1,
       option = c("bin", "cloud", "smooth"),
       estimator.type = c("classical", "robust"),
       nugget.tolerance = 0, max.dist = NULL, pairs.min = 2,
       bin.cloud = FALSE, ...)
```

Arguments

geodata	a list containing element `coords` as described next. Typically an object of the class `"geodata"` - a **geoR** data-set. If not provided the arguments `coords` must be provided instead.
coords	an $n \times 2$ matrix containing coordinates of the n data locations in each row. Defaults to `geodata$coords`, if provided.
data	a vector or matrix with data values. If a matrix is provided, each column is regarded as one variable or realization. Defaults to `geodata$data`, if provided.
uvec	a vector with values defining the variogram binning. Only used when `option = "bin"`. The values of `uvec` defines the mid-points of the bins. If $uvec[1] > 0$ the first bin is: $0 < u <= uvec[2] - 0.5 * (uvec[2] - uvec[1])$. If $uvec[1] = 0$ first bin is: $0 < u <= 0.5 * uvec[1]$ and $uvec[1]$ is replaced by the midpoint of this interval.
trend	specifies the mean part of the model. The options are: `"cte"` (constant mean), `"1st"` (a first degree polynomial on the coordinates), `"2nd"` (a second degree polynomial on the coordinates), or a formula of the type `~X` where `X` is a matrix with the covariates (external trend). Defaults to `"cte"`.
lambda	values of the Box-Cox transformation parameter. Defaults to 1 (no transformation). If another value is provided the variogram is computed after transforming the data. A case of particular interest is $\lambda = 0$ which corresponds to log-transformation.
option	defines the output type: the options `"bin"` returns values of binned variogram, `"cloud"` returns the variogram cloud and `"smooth"` returns the kernel smoothed variogram. Defaults to `"bin"`.
estimator.type	
	`"classical"` computes the classical method of moments estimator and `"robust"` returns the robust variogram estimator (Cressie, 1993). Defaults to `"classical"`.

nugget.tolerance

    a numeric value. Points which are separated by a distance less than this value are considered co-located. Defaults to zero.

max.dist   a number defining a distance. Pairs of points separated for distance greater than this value are ignored in the variogram calculation. Defaults to the maximum distance between to data locations.

pairs.min   a integer number defining the minimum numbers of pairs for the bins.. If `option = "bin"` bins with number of pairs smaller than this value are ignored. Defaults to NULL.

bin.cloud   logical. If `TRUE` and `option = "bin"` the cloud values for each class are included in the output. Defaults to `FALSE`.

...   arguments to be passed to the function `ksmooth`, if `option = "smooth"`.

Details

Variograms are widely used in geostatistical analysis for exploratory purposes, to estimate covariance parameters and/or to compare theoretical and fitted models against sample variograms.

Value

An object of the `class variogram` which is a list with the following components:

u   a vector with distances.

v   a vector with estimated variogram values at distances given in u.

n   number of pairs in each bin, if `option = "bin"`.

var.mark   variance of the data.

output.type   echoes the `option` argument.

estimator.type

    echoes the type of estimator used.

n.data   number of data points.

call   the function call.

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References

Cressie, N.A.C.(1993) *Statistics for Spatial Data*, Wiley.

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`variog.model.env` and `variog.mc.env` for variogram envelopes, `olsfit` and `wlsfit` for variogram based parameter estimation and `plot.variogram` for graphical output.

Examples

```
# Loading data:
if(is.R()) data(s100)

# computing variogram:
#
# binned variogram
vario.b <- variog(s100, max.dist=1)
# variogram cloud
vario.c <- variog(s100, max.dist=1, op="cloud")
#binned variogram and stores the cloud
vario.bc <- variog(s100, max.dist=1, bin.cloud=T)
# smoothed variogram
vario.s <- variog(s100, max.dist=1, op="sm", band=0.2)

# plotting the variograms:
par(mfrow=c(2,2))
plot(vario.b, main="binned variogram")
plot(vario.c, main="variogram cloud")
plot(vario.bc, bin.cloud=T, main="clouds for binned variogram")
plot(vario.s, main="smoothed variogram")
```

---

wlsfit   *Variogram Fitting by Weighted Least Squares*

Description

Fits a variogram model to an empirical variogram. Variogram parameters are estimated by weighted least squares.

Usage

```
wlsfit(vario, ini.cov.pars,
       cov.model = c("exponential", "matern", "gaussian",
                     "spherical", "circular", "cubic", "wave",
                     "powered.exponential", "cauchy", "gneiting",
                     "gneiting.matern", "pure.nugget"),
       fix.nugget = FALSE, nugget = 0, kappa = NULL,
       simul.number = NULL, max.dist = "all",
       minimisation.function = c("optim", "nlm"),  lower = 0,
       weight = c("npairs", "cressie"), messages.screen = TRUE)
```

Arguments

vario   an object of the class "variogram", typically an output of the function
               variog. The object is a list with information about the empirical vari-
               ogram.

ini.cov.pars   initial values for the covariance parameters: σ^2 (partial sill) and ϕ (range
               parameter). See DETAILS below.

`cov.model`	a string with the name of the correlation function. For further details see documentation for `cov.spatial`. Defaults to `"exponential"`.
`fix.nugget`	logical, indicating whether the parameter τ^2 (nugget variance) should be regarded as fixed (`fix.nugget = TRUE`) or should be estimated (`fix.nugget = FALSE`). Defaults to `FALSE`.
`nugget`	value for the nugget parameter. Regarded as a fixed values if `fix.nugget = TRUE` or as a initial value for the minimization algorithm if `fix.nugget = FALSE`. Defaults to zero.
`kappa`	fixed value of the smoothness parameter, only required by the following correlation functions: `"matern"`, `"powered.exponential"`, `"gneiting"` and `"gneiting.matern"`.
`simul.number`	number of simulation. To be used when the object passed to the argument `vario` has empirical variograms for more than one data-set (or simulation). Indicates to which one the model will be fitted.
`max.dist`	maximum distance considered when fitting the variogram. Defaults to `vario$max.dist`.
`minimisation.function`	
	minimization function used to estimate the parameters. Options are `"optim"` and `"nlm"`. Defaults to `"optim"`.
`lower`	lower limits for the parameter values. Defaults to zero.
`weight`	type weights used in the loss function. See `DETAILS` below.
`messages.screen`	
	logical. Indicates whether or not status messages are printed on the screen (or other output device) while the function is running.
`...`	further parameters to be passed to the minimization function. Typically arguments of the type `control()` which controls the behavior of the minimization algorithm. See documentation for the selected minimization function for further details.

Details

Initial values

The algorithms for minimization functions require initial values of the parameters.

A unique initial value is used if a vector is provided in the argument `ini.cov.pars`. The elements are initial values for σ^2 and ϕ, respectively. This vector is concatenated with the value of the argument `nugget` if `fix.nugget = FALSE`.

Specification of multiple initial values is also possible. If this is the case, the function searches for the one which minimizes the loss function and uses this as the initial value for the minimization algorithm. Multiple initial values are specified by providing a matrix in the argument `ini.cov.pars` and/or, if `fix.nugget = FALSE`, providing a vector with length greater than one for the argument `nugget`. If `ini.cov.pars` is a matrix, the first column has values of σ^2 and the second has values of ϕ.

Weights

Two different types of weights can be used within the loss function:

`"npairs"` indicating that the weights are given by the number of pairs in each bin.

`"cressie"` weights as suggested by Cressie (1993, p.95).

See also Barry, Crowder and Diggle (1997) for a discussion on the methods to estimate variogram parameters.

Value

An object of the `class "variomodel"` which is list with the following components:

`nugget`	value of the nugget parameter. An estimated value if `fix.nugget = FALSE` or a fixed value if `fix.nugget = TRUE`.
`cov.pars`	a 2 elements vector with estimated values of the covariance parameters σ^2 and ϕ, respectively.
`cov.model`	a string with the name of the correlation function.
`kappa`	fixed value of the smoothness parameter.
`value`	minimized value of the loss function.
`max.dist`	maximum distance considered in the variogram fitting.
`minimisation.function`	minimization function used.
`message`	status messages returned by the function.
`method`	a string `"WLS"` indicating the estimation method.
`call`	the function call.

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References

Barry, J.T., Crowder, M.J. and Diggle, P.J. (1997) Parametric estimation of the variogram. *Tech. Report, Dept Maths & Stats, Lancaster University.*

Cressie, N.A.C (1993) *Statistics for Spatial Data.* New York: Wiley.

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.

See Also

`cov.spatial` for a detailed description of the available correlation (variogram) functions, `olsfit` for ordinary least squares variogram fit, `likfit` for maximum and restricted maximum likelihood estimation, `lines.variomodel` for graphical output of the fitted model. For details on the minimization functions see documentation for `optim` and `nlm`.

Examples

```
if(is.R()) data(s100)
vario100 <- variog(s100, max.dist=1)
ini.vals <- expand.grid(seq(0,1,l=5), seq(0,1,l=5))
wls <- wlsfit(vario100, ini=ini.vals, fix.nug=TRUE)
summary(wls)
plot(vario100)
lines(wls)
```

---

wrappers   *Wrappers for the C functions used in geoR*

Description

These functions are *wrappers* for some, but no tall, the C functions included in the **geoR** package.
Typically the C code is directly called from the **geoR** functions but these functions allows independent calls.

Usage

```
distdiag(coords)
loccoords(coords, locations)
diagquadraticformXAX(X, lowerA, diagA)
bilinearform(X, lowerA, diagA, Y)
```

Arguments

coords	an $n \times 2$ matrix with the data coordinates.
locations	an $n \times 2$ matrix with the coordinates of the prediction locations.
lowerA	a vector with the diagonal terms of the symmetric matrix A.
diagA	a vector with the diagonal terms of the symmetric matrix A.
X	a matrix with conforming dimensions.
Y	a matrix with conforming dimensions.

Value

The outputs are:

loccoords	returns a vector with distances between data points and prediction locations.
distdiag	returns a vector with distances between data locations, including the diagonal zero values.
diagquadraticformXAX	
	returns a vector with the diagonal term of the quadratic form $X'AX$.
bilinearform	returns a vector or a matrix with the terms of the quadratic form $X'AY$.

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References

Further information about **geoR** can be found at:
http://www.maths.lancs.ac.uk/~ribeiro/geoR.html.